

Continuum Reverberation of Accretion Disks Surrounding Low-Mass-Ratio SMBHBs

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“VII Conference on AGN and Gravitational Lensing”
Serbia, 2026-07-21

Outline

- Brief introduction to SMBHBs
- Continuum reverberation of SMBHB accretion disks
- Application to PG 1302-102
- Future perspective

The life history of SMBHBs



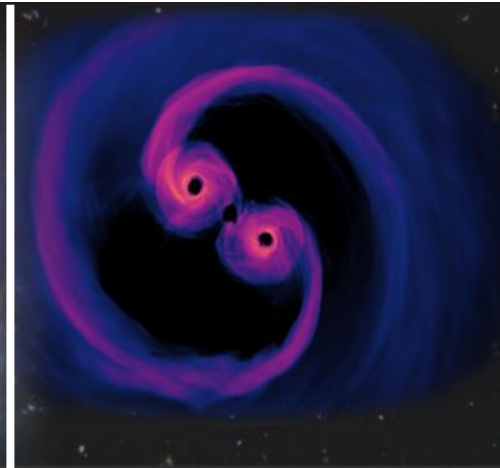
galaxy merger

$> \text{kpc}$



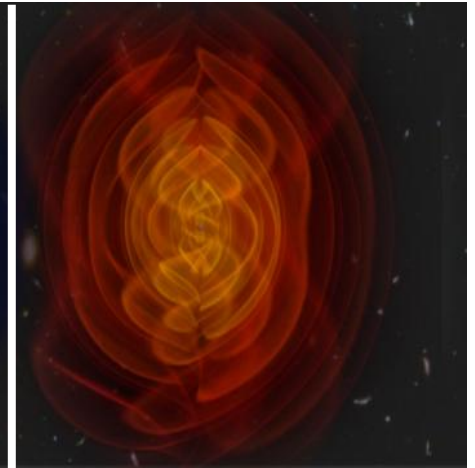
dual AGN

$\sim 100 \text{ pc} - \text{kpc}$

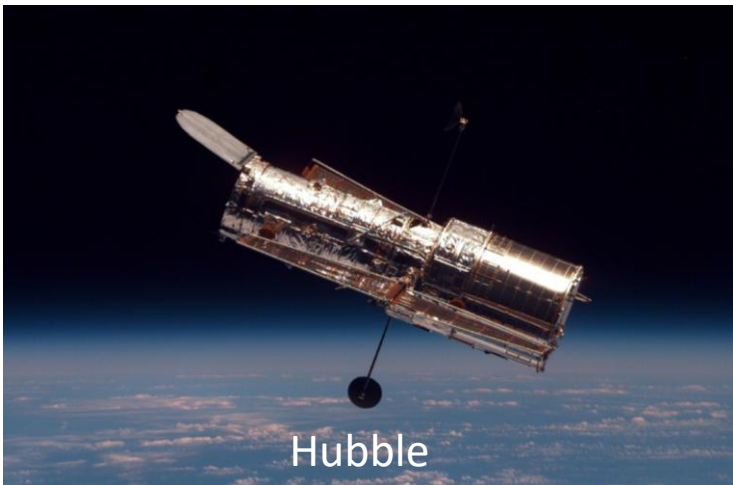


SMBHB

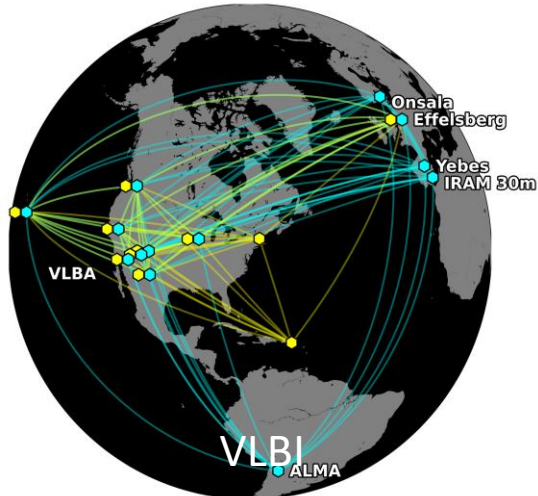
$< 1 \text{ pc}$



coalescence



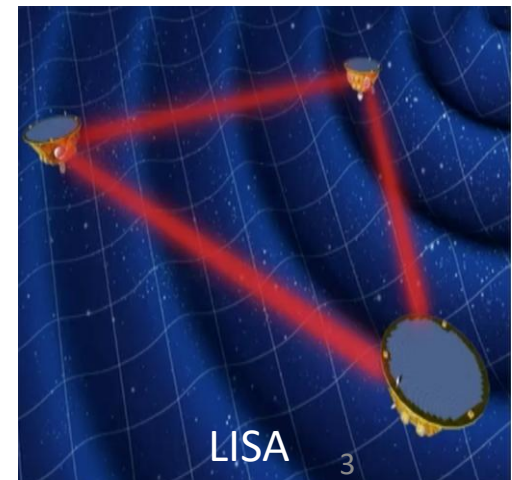
Hubble



VLBI



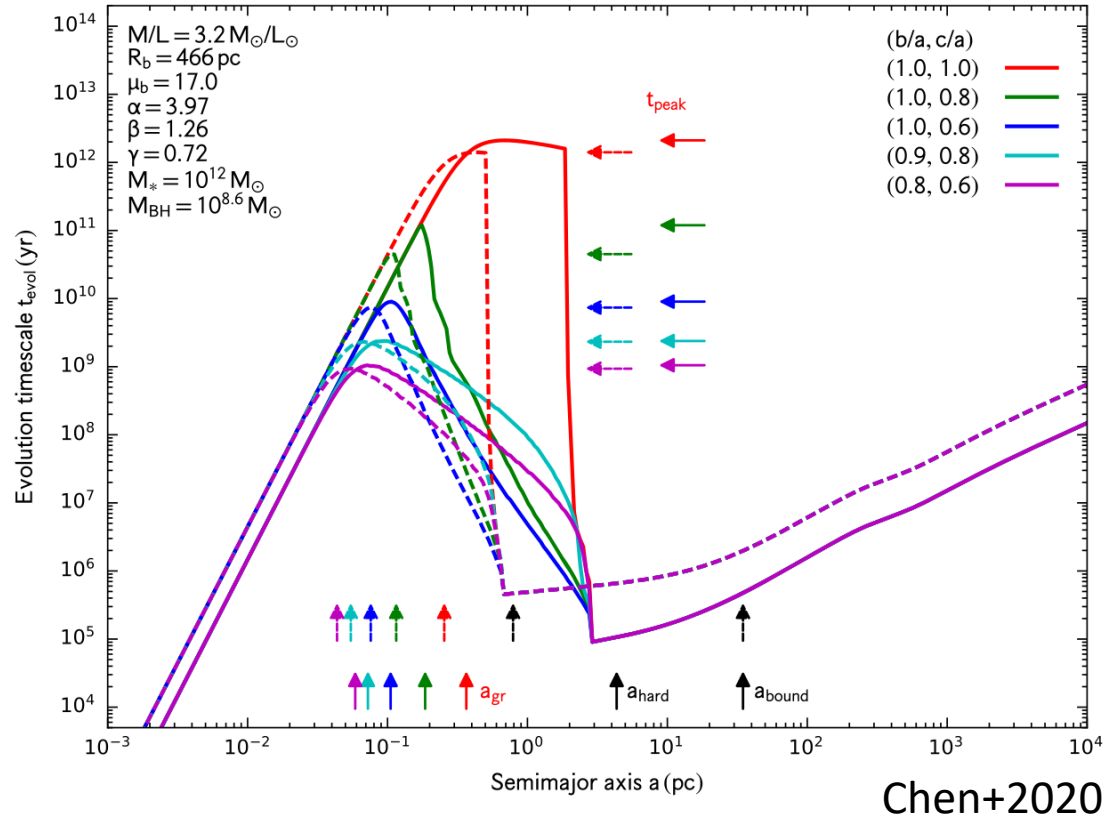
PTA



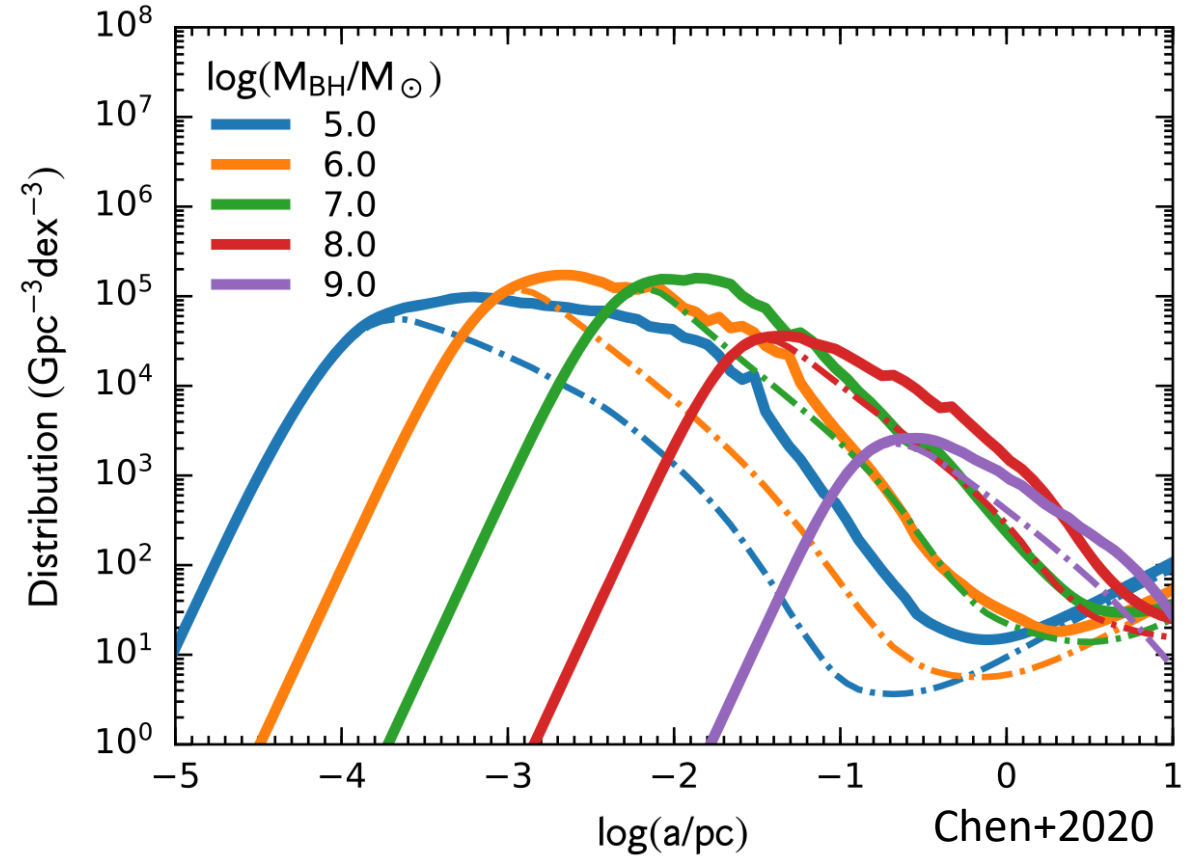
LISA

The life history of SMBHBs

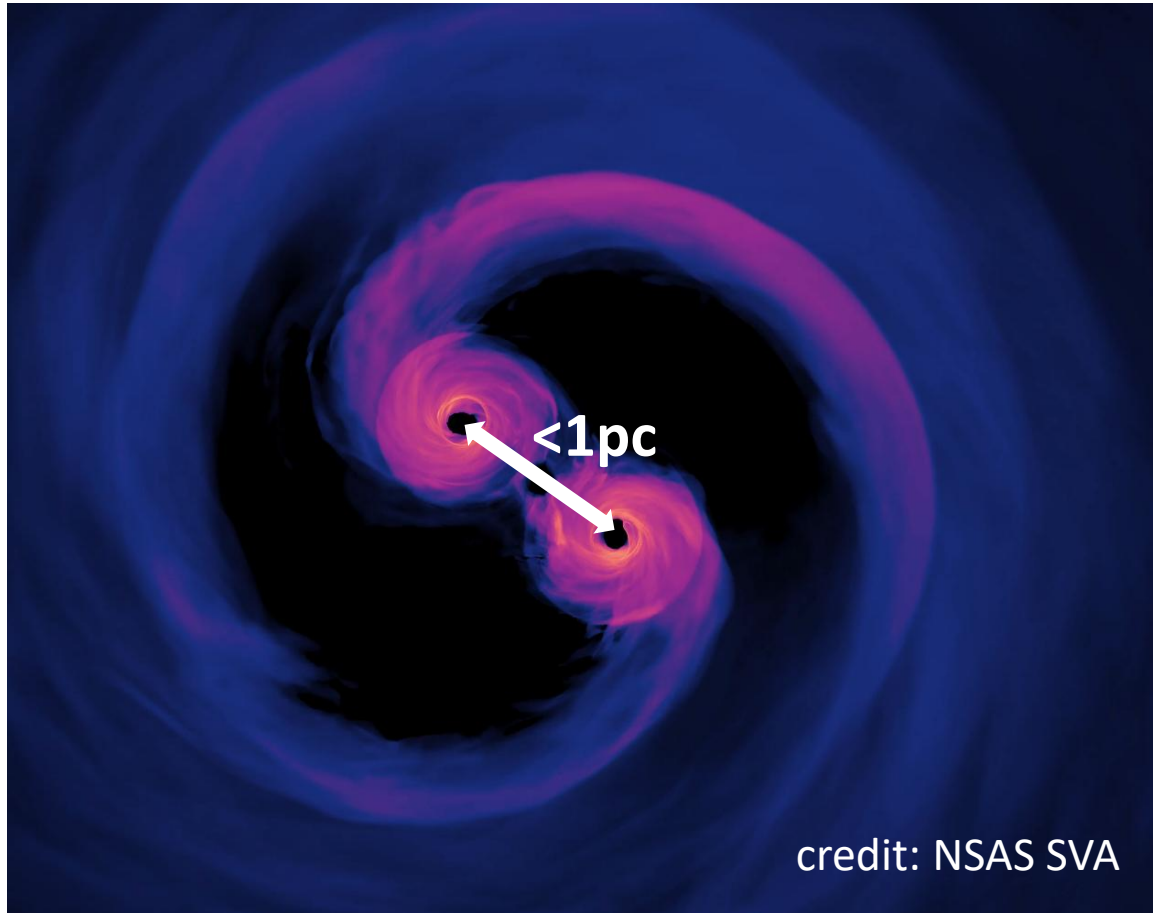
Evolution timescale



orbital separation distribution at $z=0$



Electromagnetic identification of SMBHBs is challenging...



1pc at $z=0.4$ (cosmic distance=1Gpc)

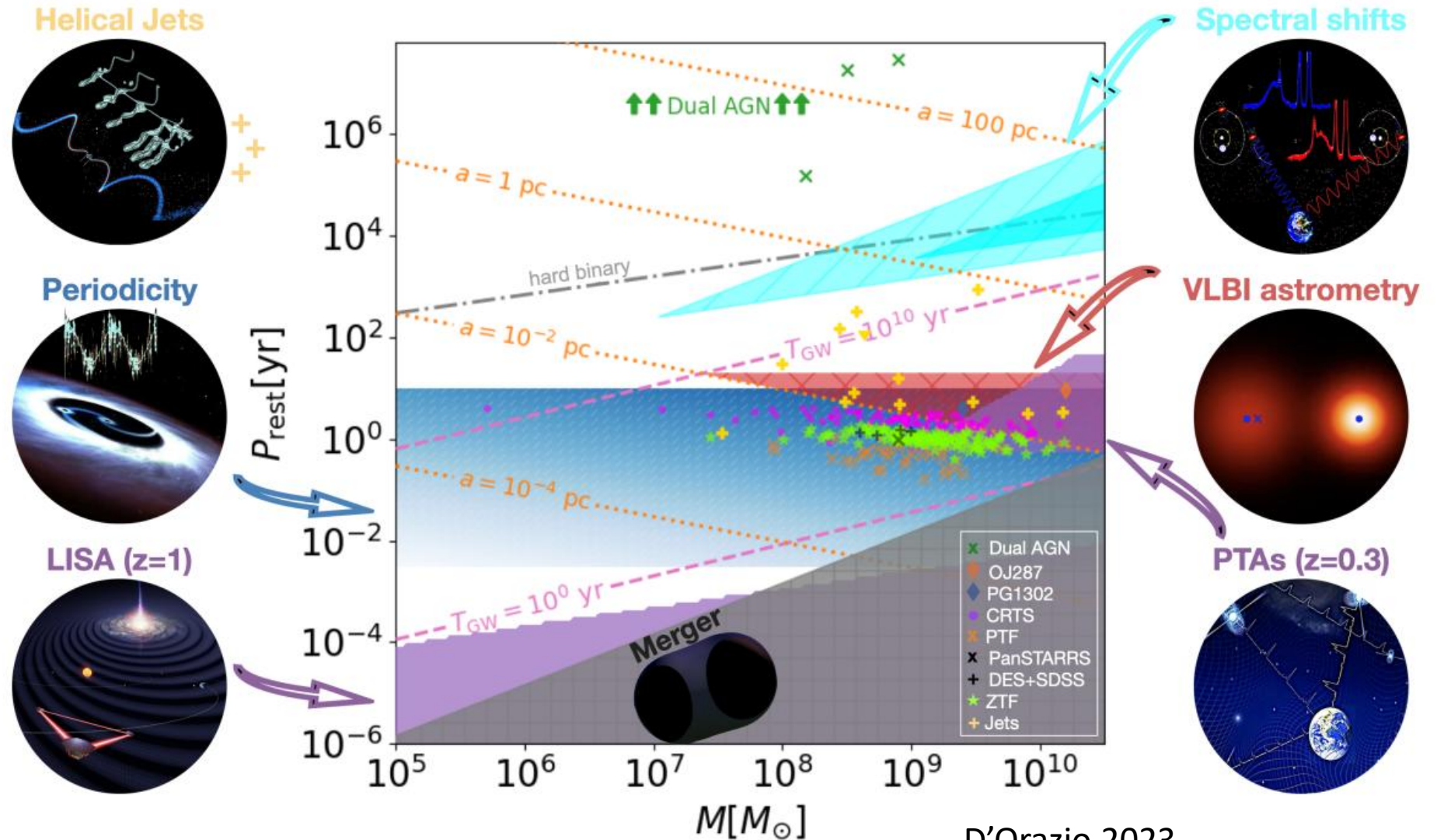
angular size: ~ 0.2 milli-arcsec

JWST 6m: ~ 70 milli-arcsec @ $2\mu\text{m}$

ELT 39m: ~ 10 milli-arcsec @ $2\mu\text{m}$

Many indirect identification methods are proposed

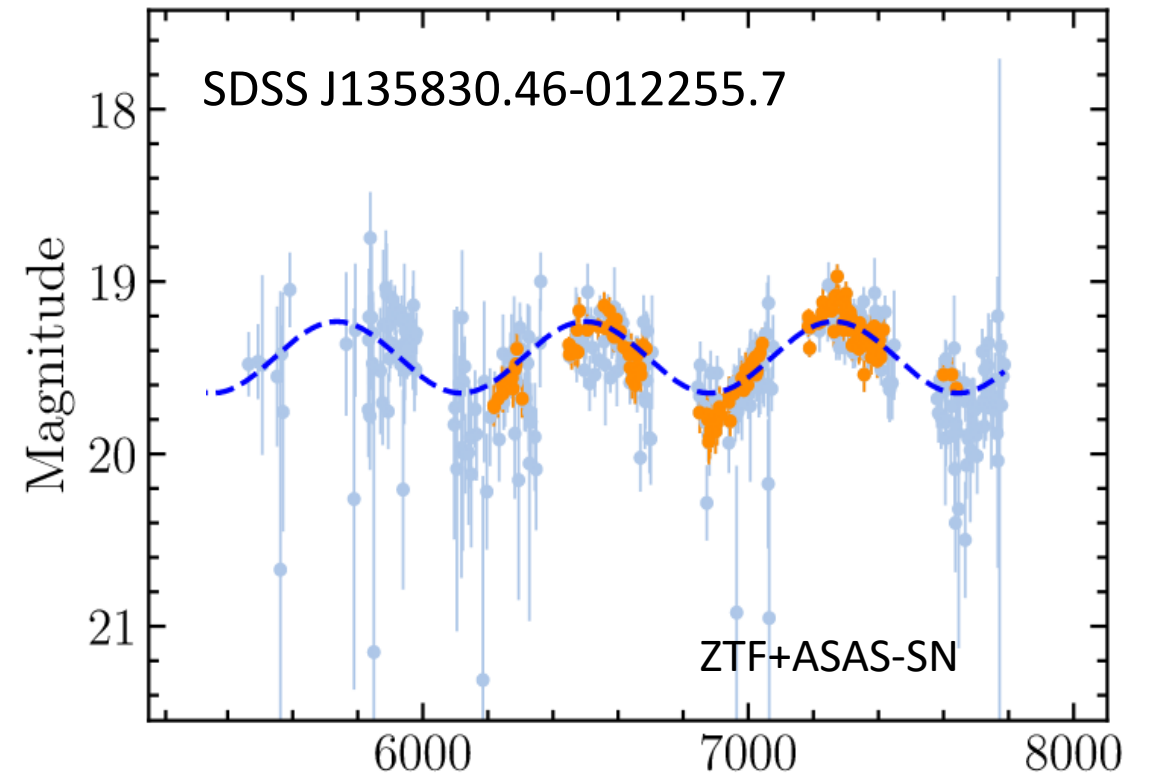
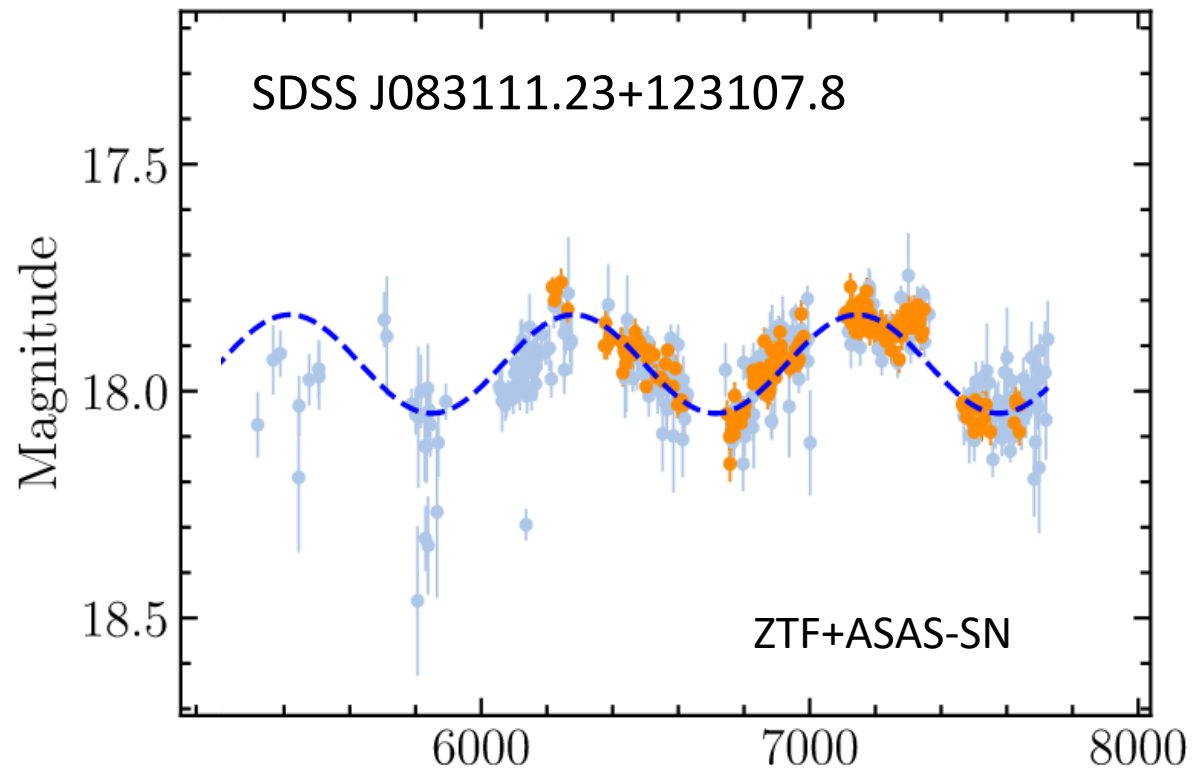
- Periodical variability
- UV deficiency
- X-shaped/helical jet
- Broad-line signatures
- Self-lensing variations
- Tidal disruption
- etc



D'Orazio 2023

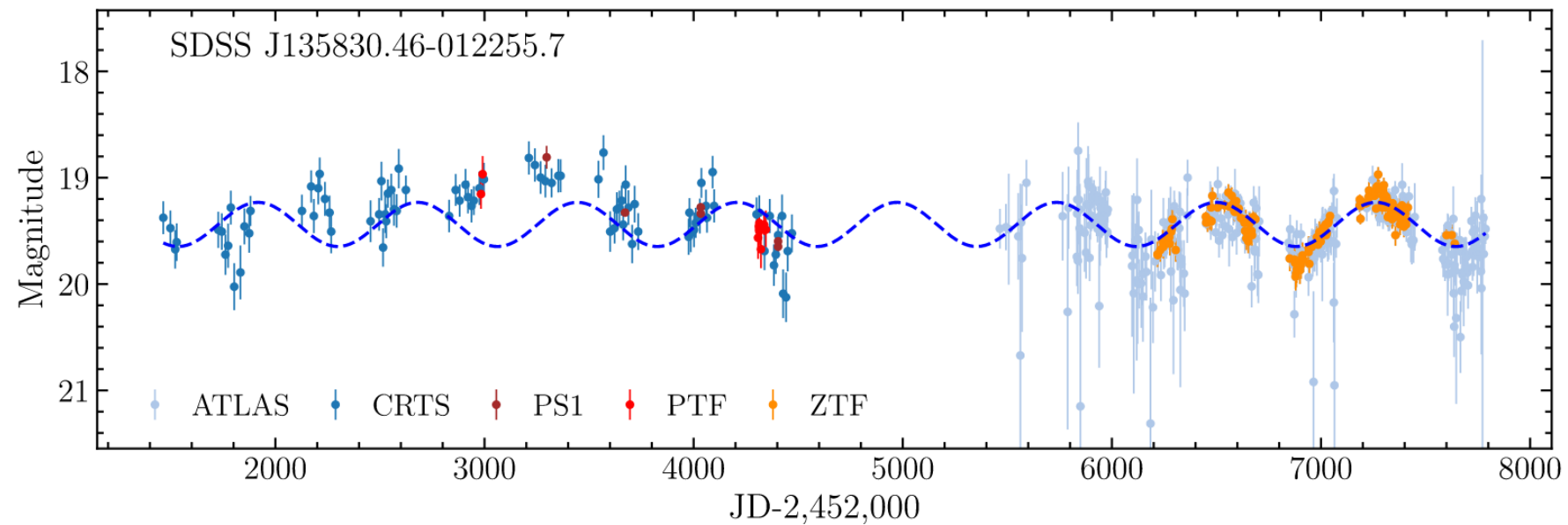
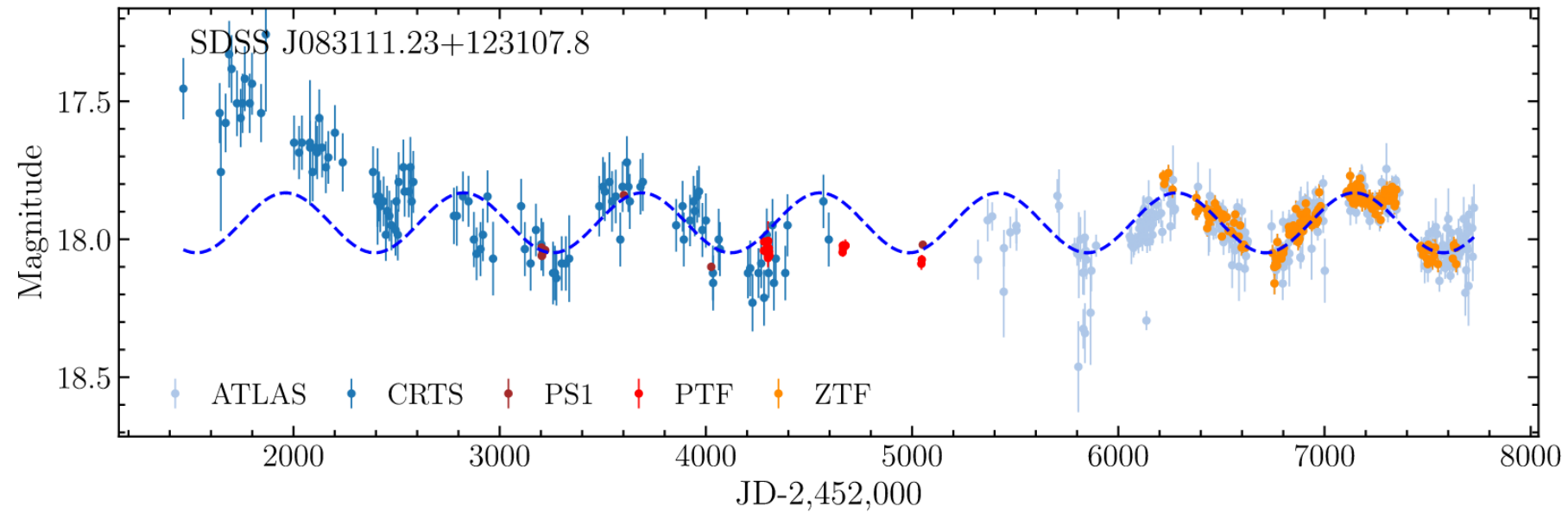
Periodical searches for SMBHBs

Graham et al. 2015; Charisi et al. 2016; Liu et al. 2019; Chen et al. 2020; Chen et al. 2024

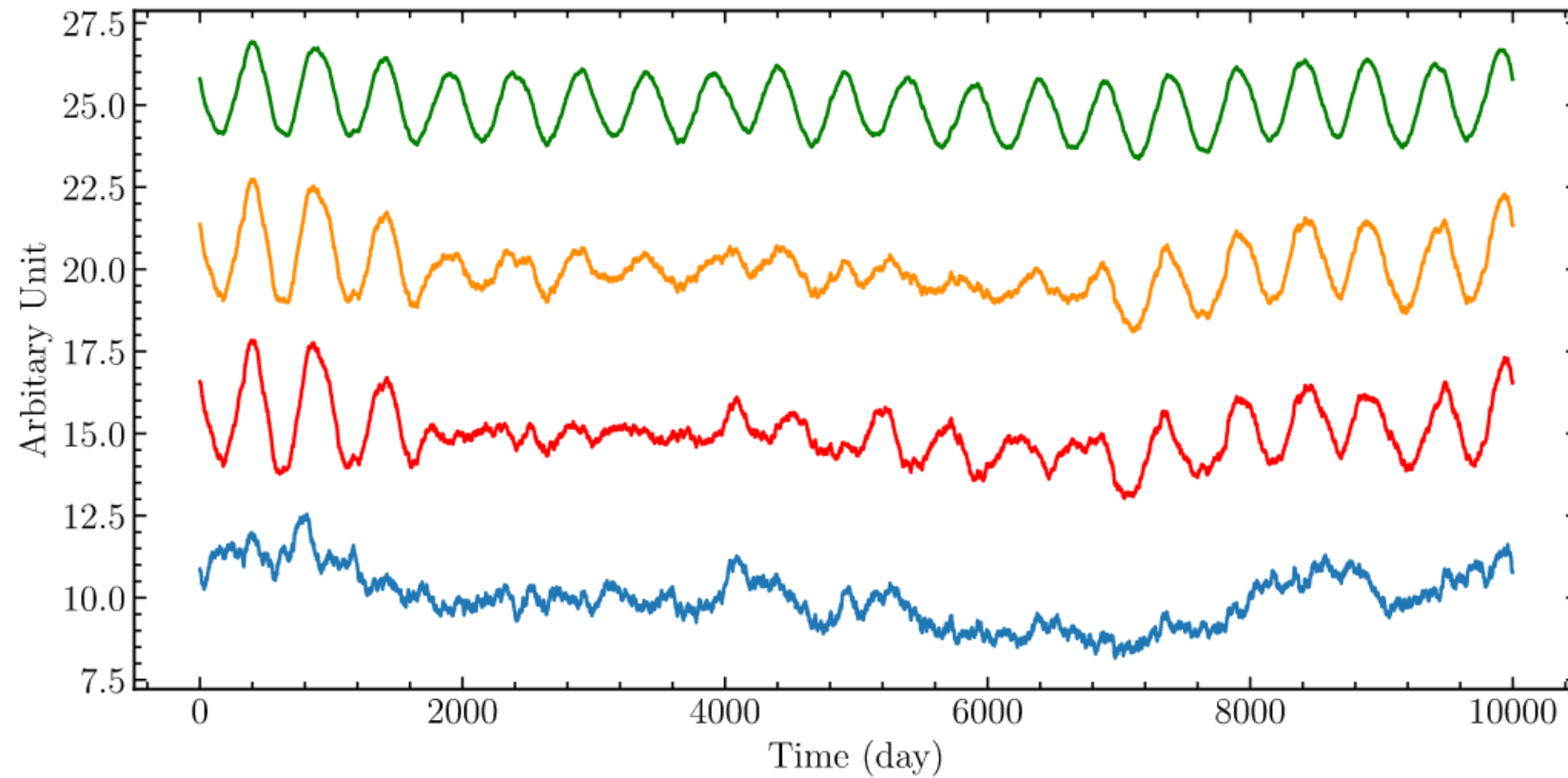


Chen et al. (LYR) 2024

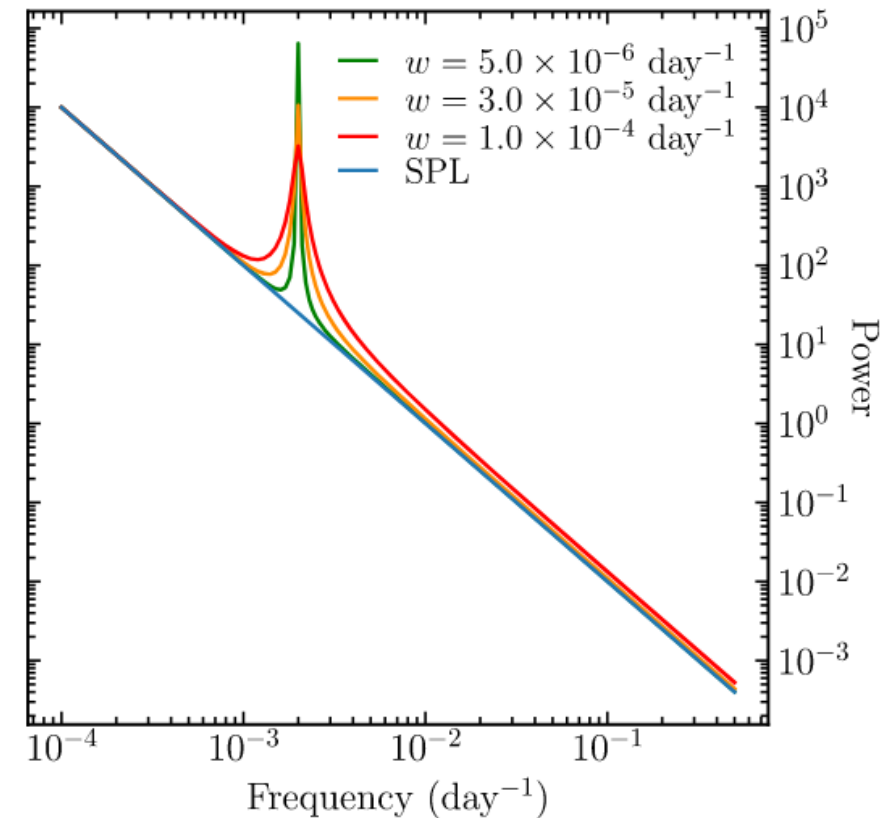
Periodical searches for SMBHBs



Explanation: quasi-periodical + red-noise variability

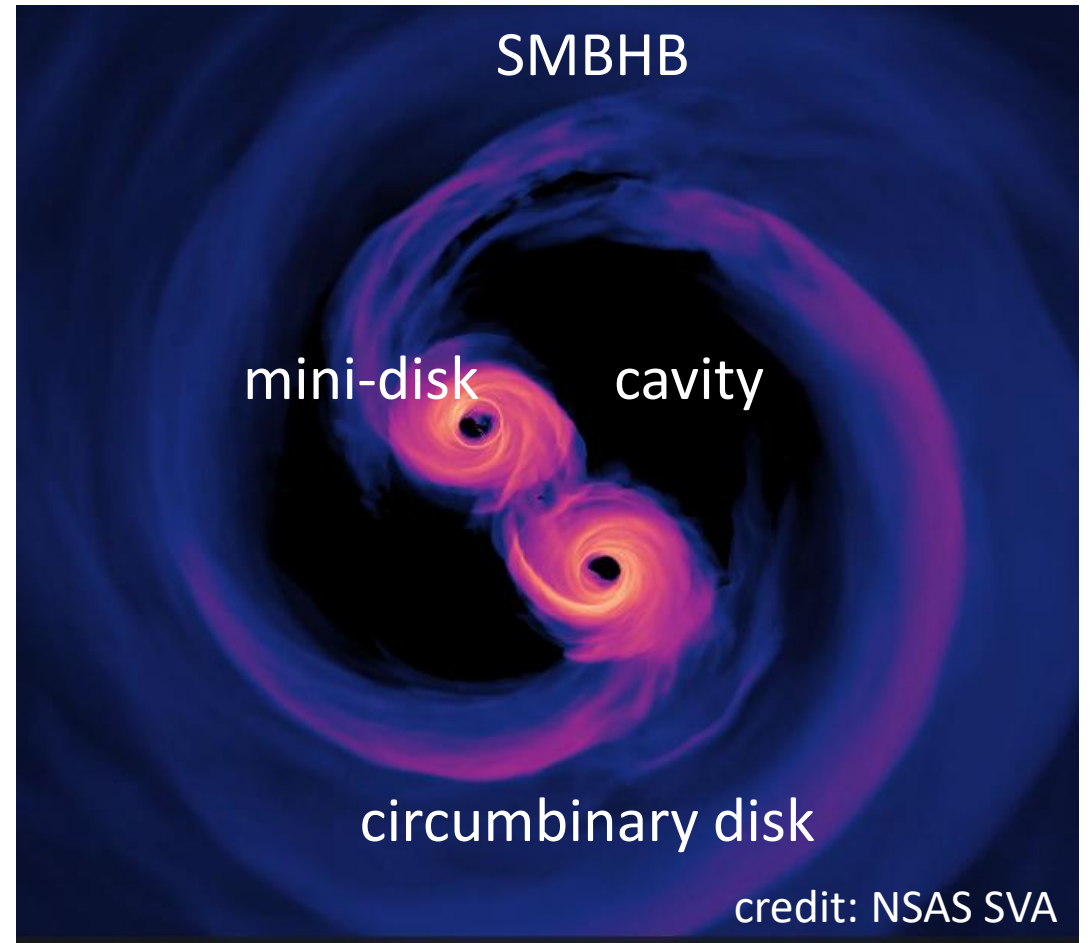
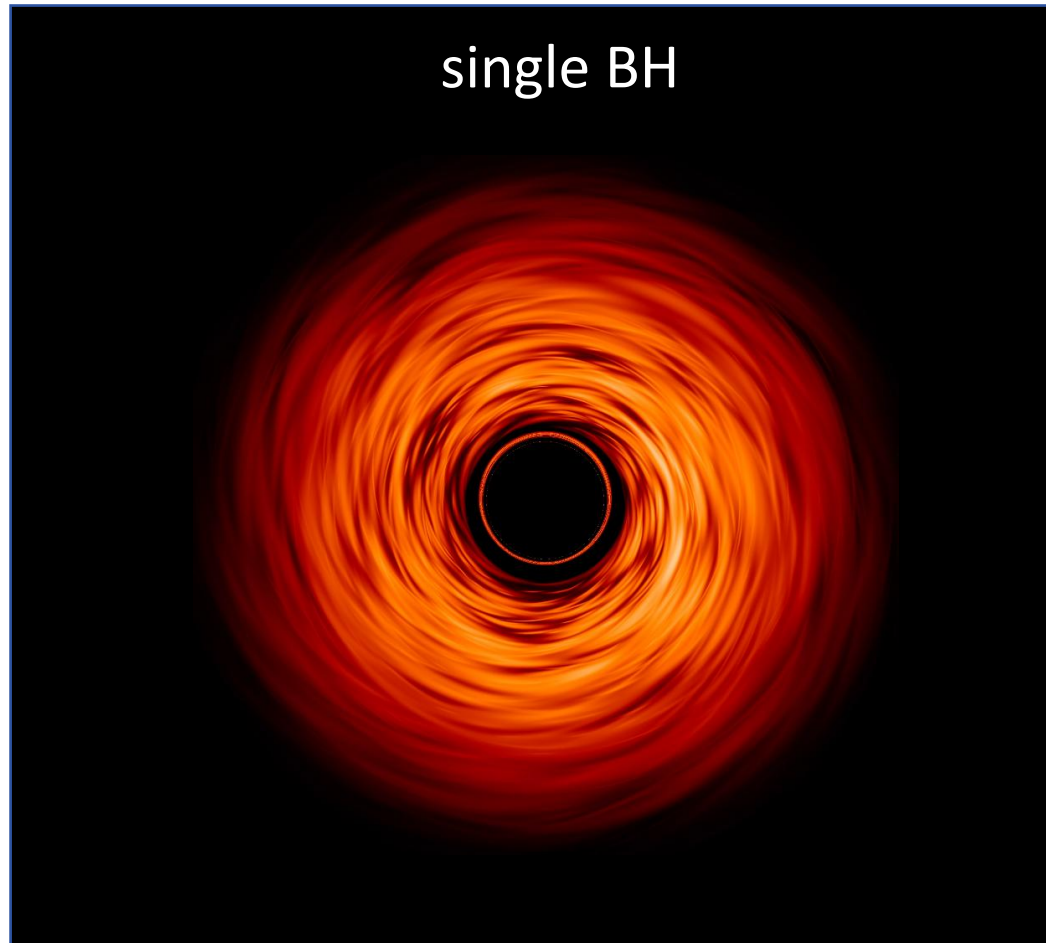


light curves



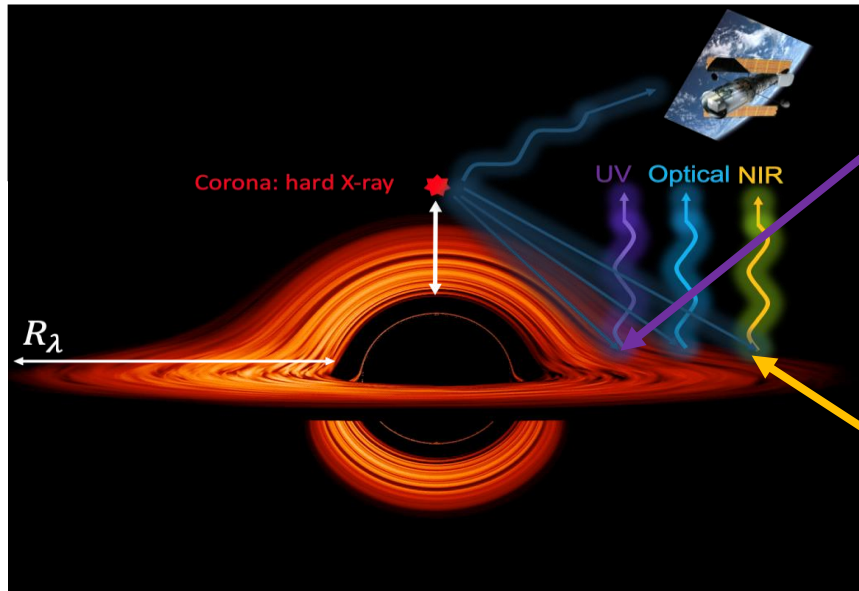
power spectral density

Basic concept: accretion disks surrounding SMBHBs

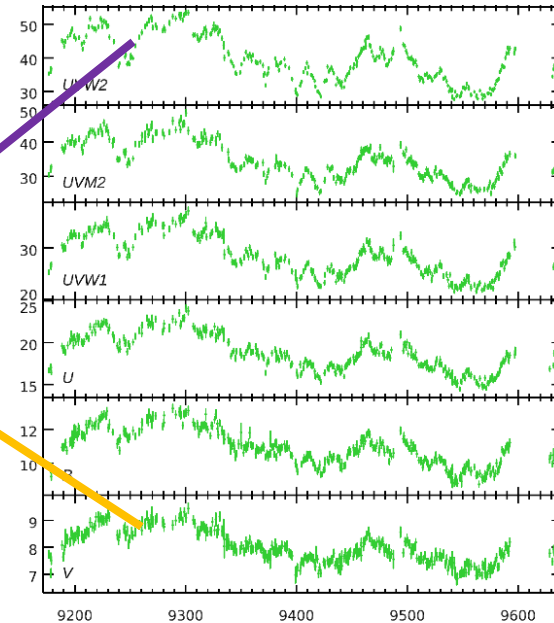


Reverberation Mapping: measuring disk structure

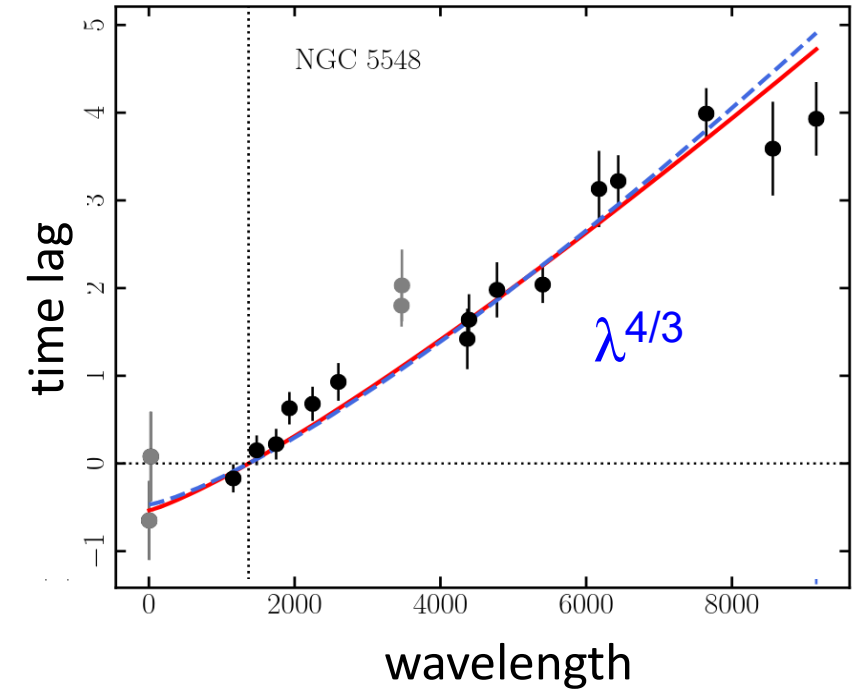
$$X(\lambda, t) = \int_0^\infty \psi(\lambda, \tau) X_b(t - \tau) d\tau \quad \psi(\lambda, \tau) \equiv A(\lambda) \int_\Sigma \frac{\partial B(\lambda, T)}{\partial T} \frac{\partial T}{\partial L_b} \delta(\tau_d - \tau) r d\theta dr$$



accretion disk + lamp-post



light curves



Reverberation mapping: measuring disk structure

viscous energy

$$Q_{\text{vis}} = \frac{3GM\dot{M}}{4\pi r^3} \left(1 - \sqrt{\frac{r_{\text{ISCO}}}{r}} \right)$$

time lag

$$\tau_d(r, \theta) = \frac{1}{c} (\sqrt{r^2 + h^2} - r \cos \theta \sin i + h \cos i) \sim r/c$$

lamp-post illumination

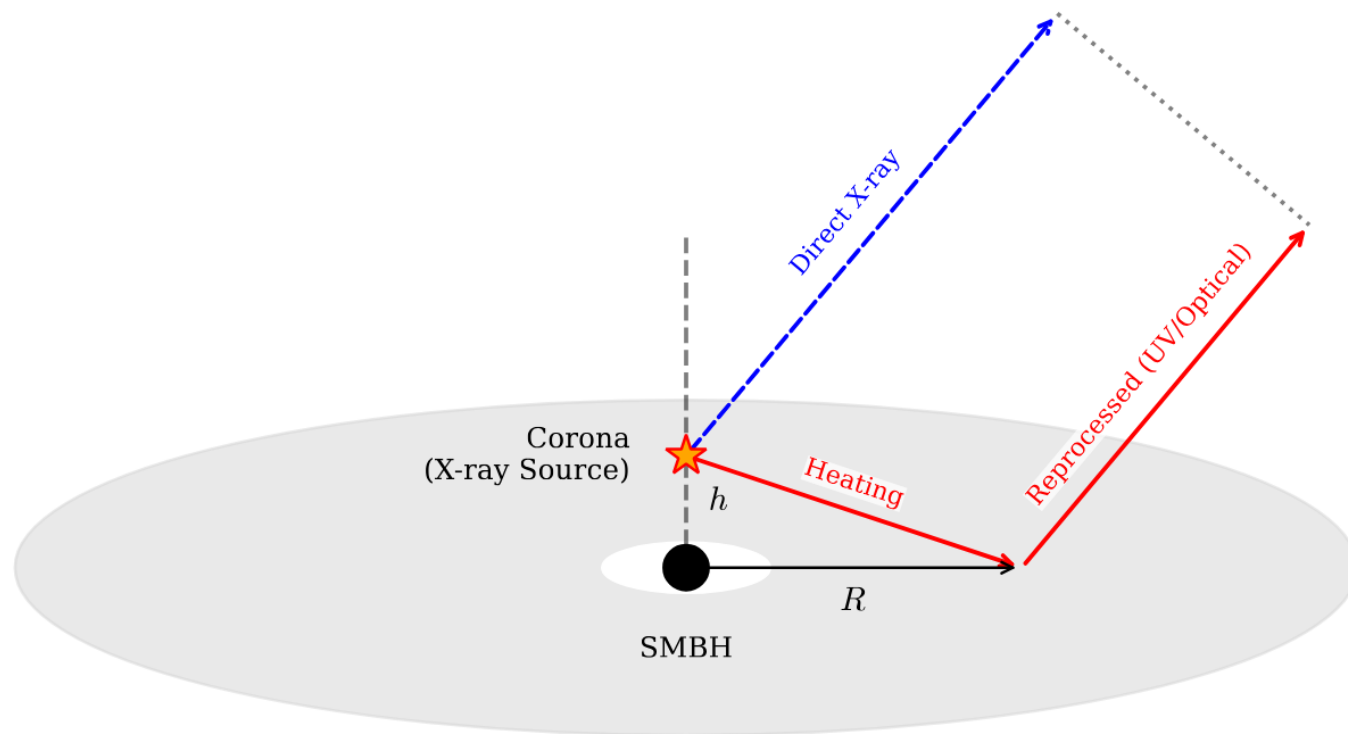
$$Q_{\text{lp}}(r, t) = \frac{2(1-a)L_b(t - \tau_1)}{4\pi(r^2 + h^2)} \cos \theta_{\text{inc}}$$

thermal balance

$$2\sigma T^4(r, t) = Q_{\text{vis}}(r) + Q_{\text{lp}}(r, t)$$

temperature profile

$$T(r) \propto r^{-3/4}$$



Reverberation mapping: measuring disk structure

viscous energy

$$Q_{\text{vis}} = \frac{3GM\dot{M}}{4\pi r^3} \left(1 - \sqrt{\frac{r_{\text{ISCO}}}{r}} \right)$$

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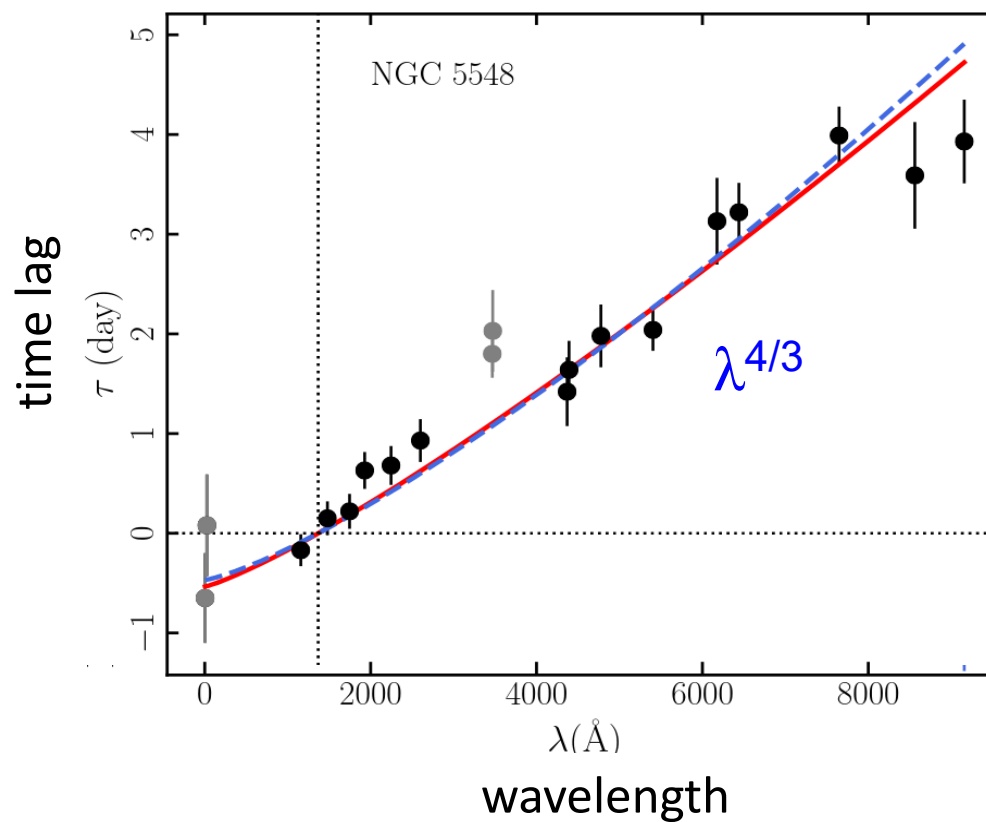
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thermal balance

$$2\sigma T^4(r, t) = Q_{\text{vis}}(r) + Q_{\text{lp}}(r, t)$$

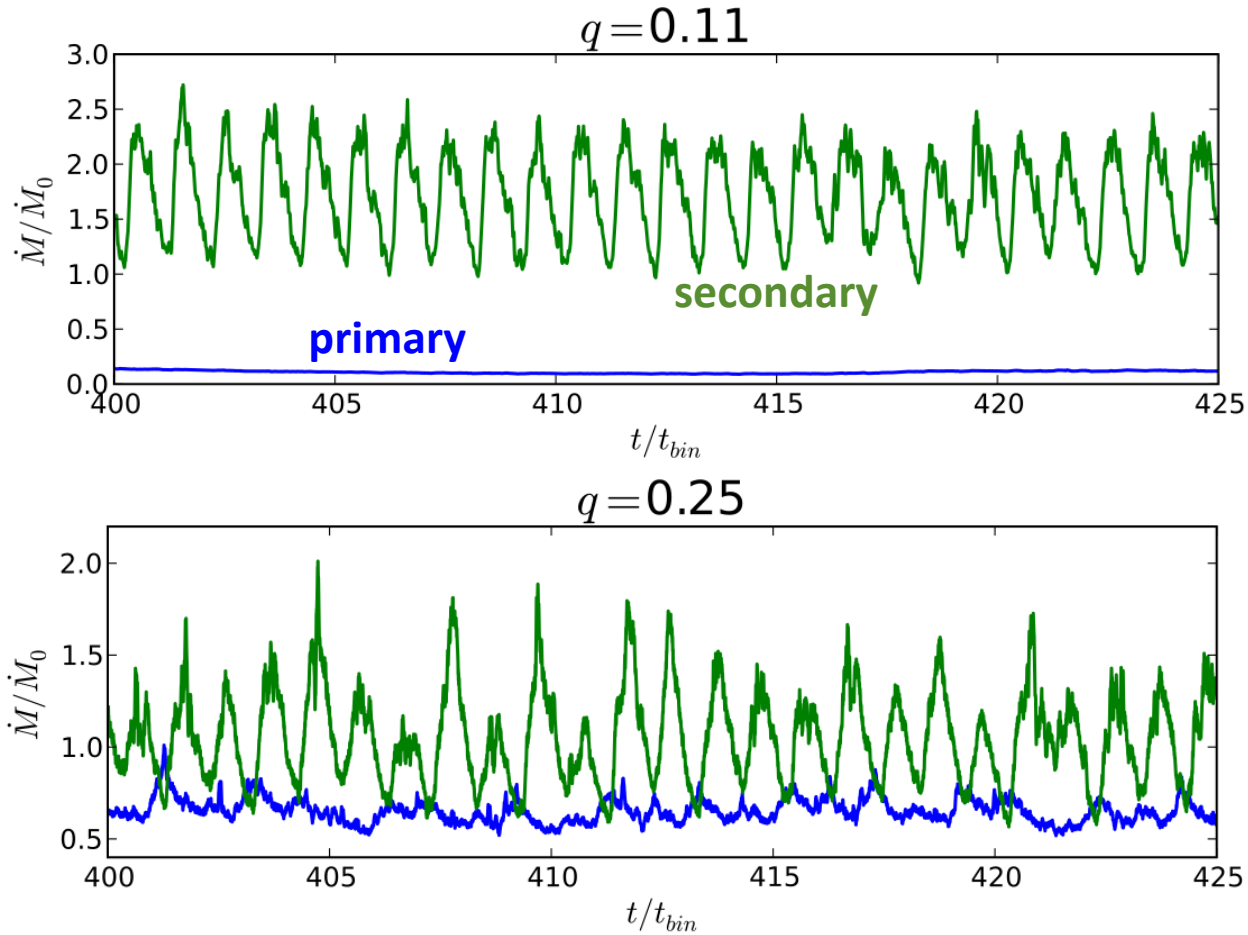
temperature profile

$$T(r) \propto r^{-3/4}$$

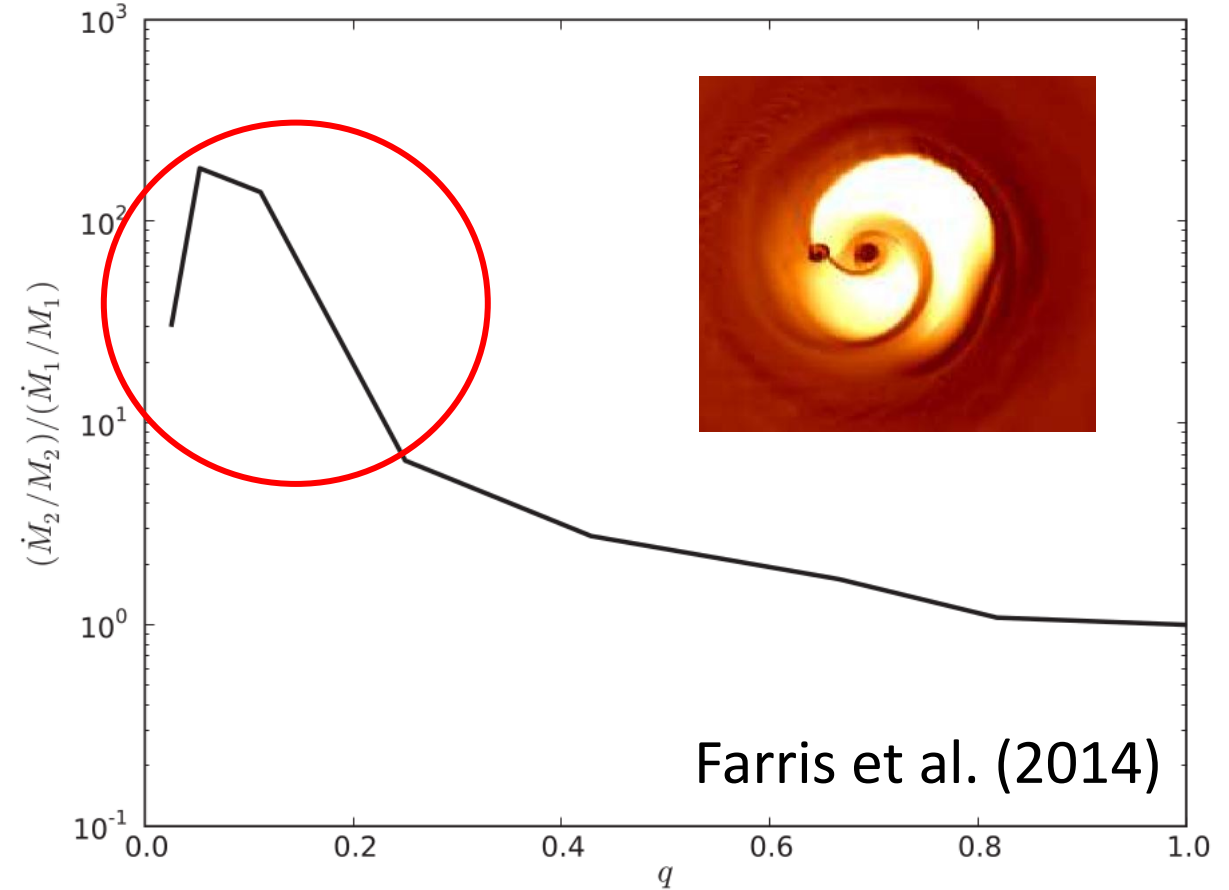


Low-mass-ratio SMBHBs: secondary BH is more active

variations of accretion rates

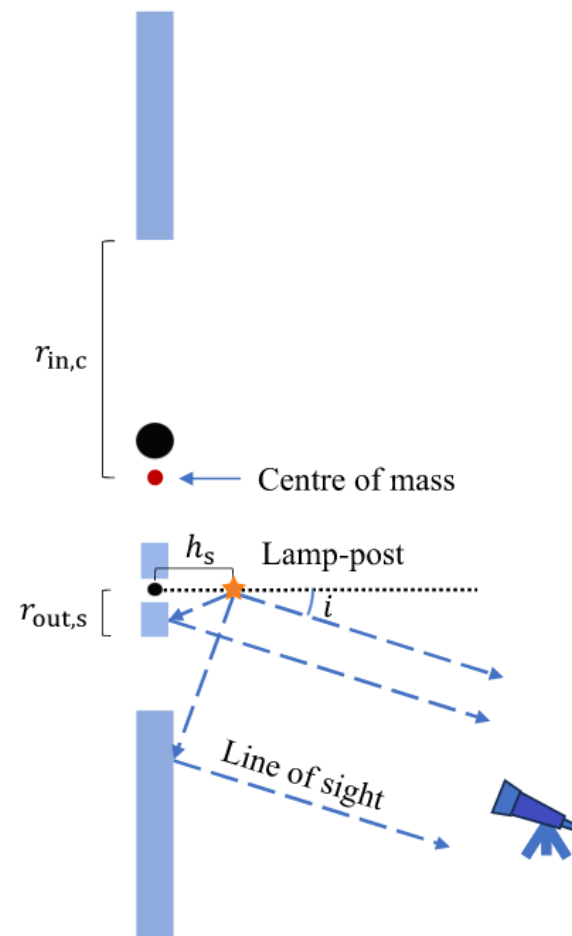
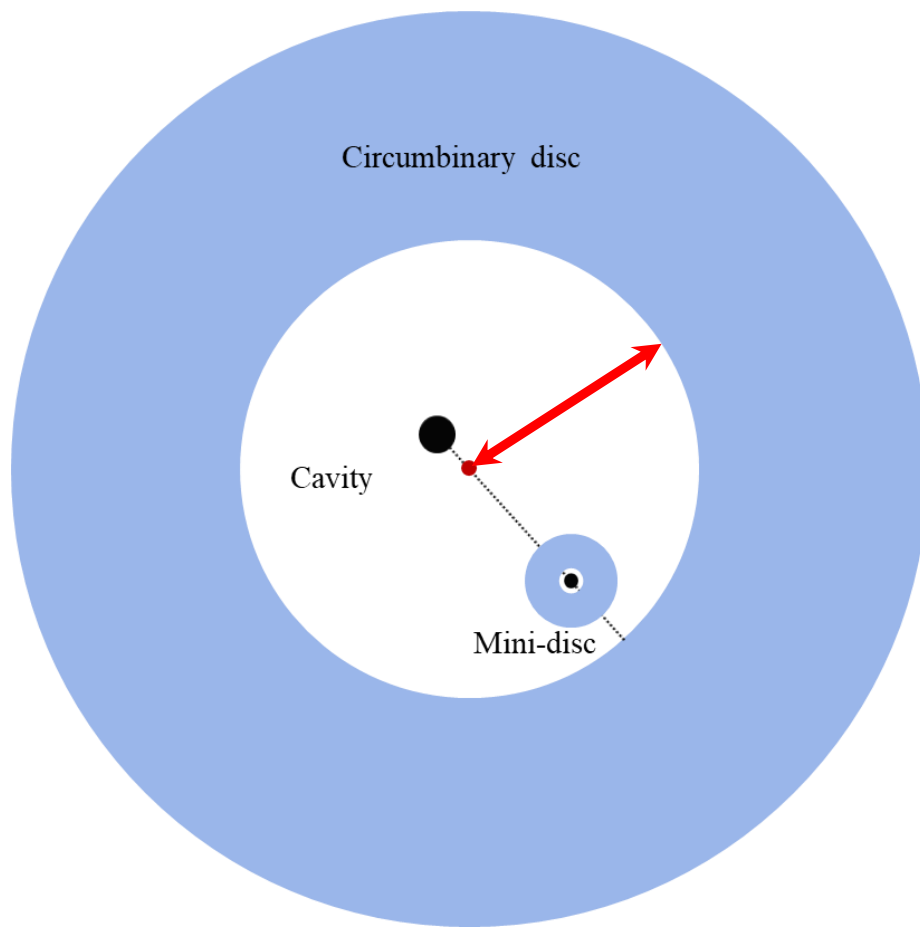


ratio of accretion rates



Low-mass-ratio SMBHBs model

- mass ratio $q \leq 0.25$
- circular Keplerian orbit
- only secondary BH is active
- circular cavity
size: $\sim 2a$
- mini-disk is truncated
size: a fraction of Roch lobe
- lamp-post scenario



Low-mass-ratio SMBHBs model

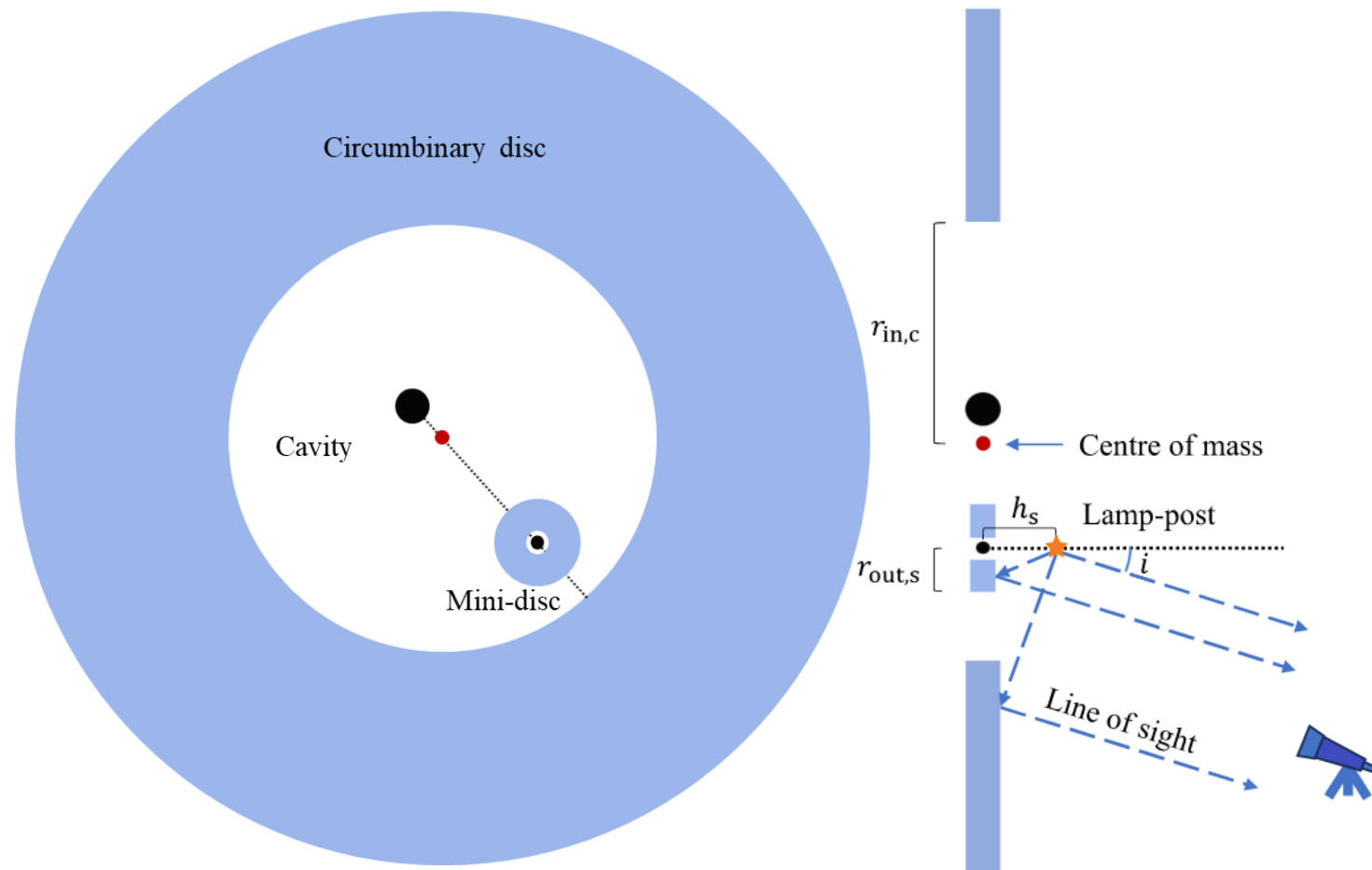
Disk surface temperature:

$$T^4(t, \mathbf{r}) = T_{\text{vis}}^4(\mathbf{x}) + T_{\text{b}}^4(t - \tau, \mathbf{r})$$

$$T_{\text{vis}}^4 = \begin{cases} \frac{3GM_s\dot{M}_s}{8\pi\sigma r^3} \left(1 - \sqrt{\frac{r_{\text{in},s}}{r}}\right) \\ \frac{3GM_t\dot{M}_c}{8\pi\sigma r_c^3} \end{cases}$$

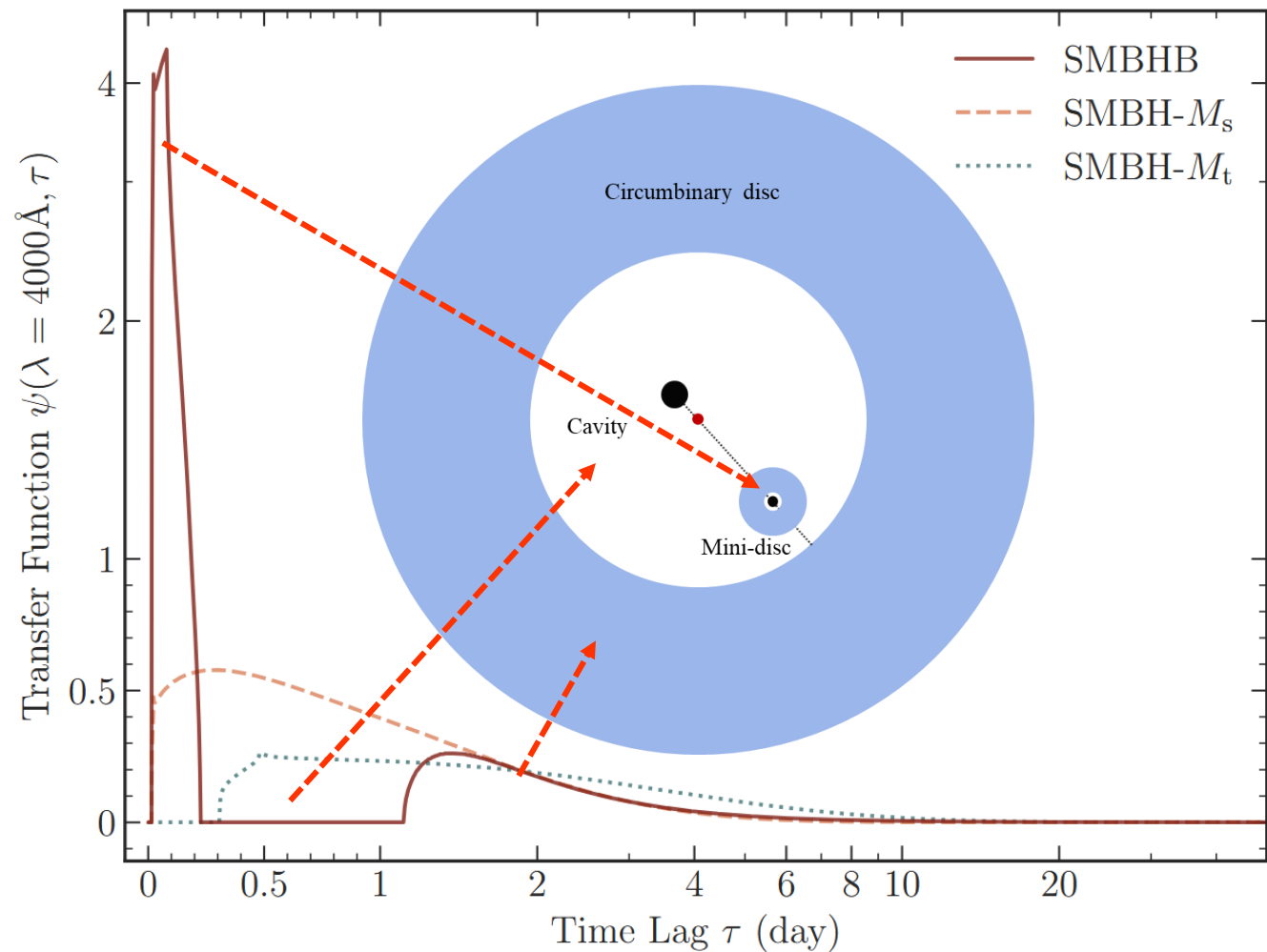
$$T_{\text{b}}^4(t - \tau_s) = \frac{L_{\text{b}}(t - \tau_s)(1 - a)h_s}{4\pi\sigma} \times \begin{cases} (r^2 + h_s^2)^{-3/2} \\ (d_c^2 + h_s^2)^{-3/2} \end{cases}$$

$$\psi(\lambda, \tau) \equiv A(\lambda) \int_{\Sigma} \frac{\partial B(\lambda, T)}{\partial T} \frac{\partial T}{\partial L_{\text{b}}} \delta(\tau_{\text{d}} - \tau) r d\theta dr$$



Low-mass-ratio SMBHBs: two-mode transfer function

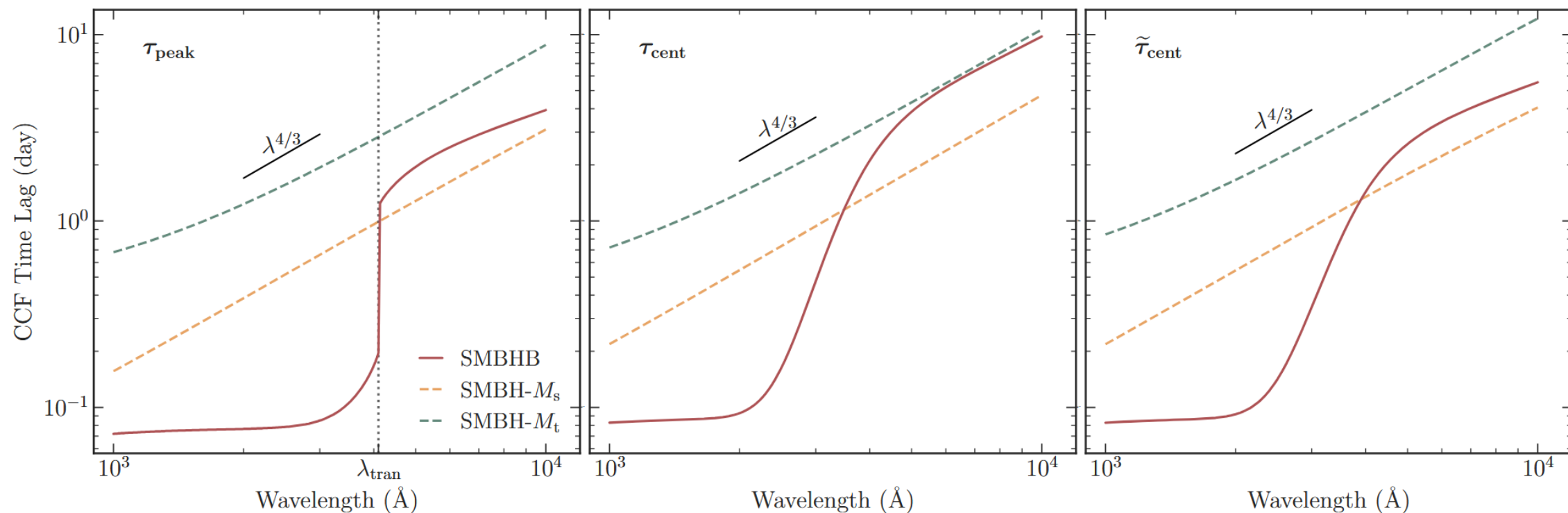
Parameter	Unit	Value
M_t	$10^8 M_\odot$	5.25
M_p	$10^8 M_\odot$	5
M_s	$10^8 M_\odot$	0.25
q	—	0.05
a_B	$R_{g,t}$	300
P_B	day	977
$\dot{M}_c$	$\dot{M}_{\text{Edd},c}$	0.1
$\dot{M}_s$	$\dot{M}_{\text{Edd},s}$	2.1
L_μ	$\eta \dot{M}_s c^2$	f_b
a	—	0.1
h_s	$R_{g,s}$	6
$r_{s,\text{in}}$	$R_{g,s}$	6
$r_{s,\text{out}}$	$r_{R,s}$	0.1
$r_{c,\text{in}}$	a_B	$(1+q)^{-1} + (q/3)^{1/3}$
$r_{c,\text{out}}$	$R_{g,t}$	10^5
θ_s	degree	0
i	degree	30
T_{GW}	yr	3×10^5



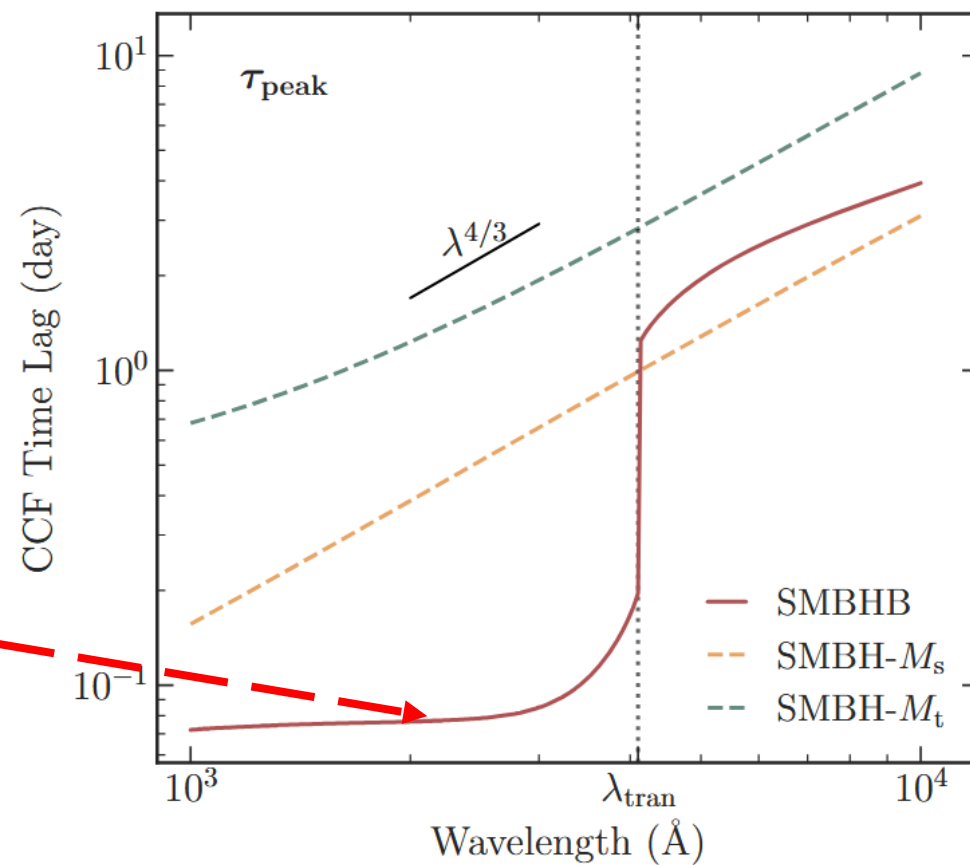
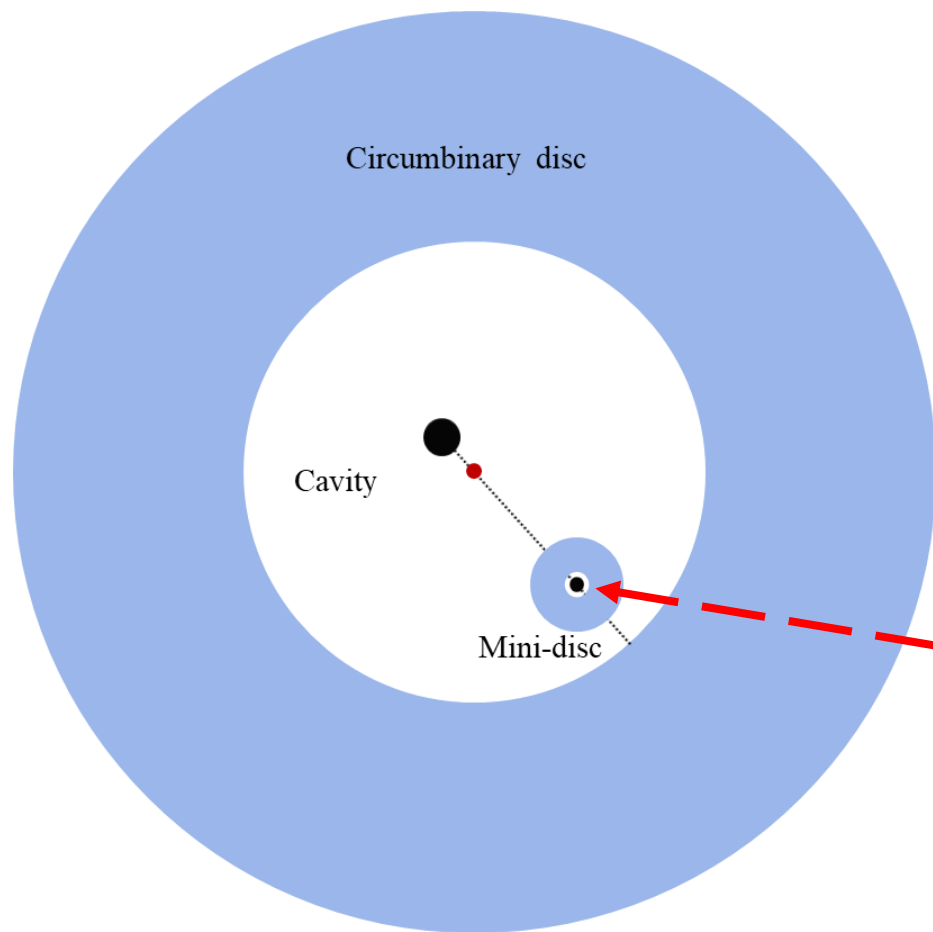
Low-mass-ratio SMBHBs: τ - λ relation

$$\tau_{\text{peak}} \equiv \arg \max \psi_{\otimes}(\lambda, \tau) \quad \tau_{\text{cent}} = \frac{\int_0^{\infty} \tau \psi_{\otimes}(\lambda, \tau) d\tau}{\int_0^{\infty} \psi_{\otimes}(\lambda, \tau) d\tau}$$

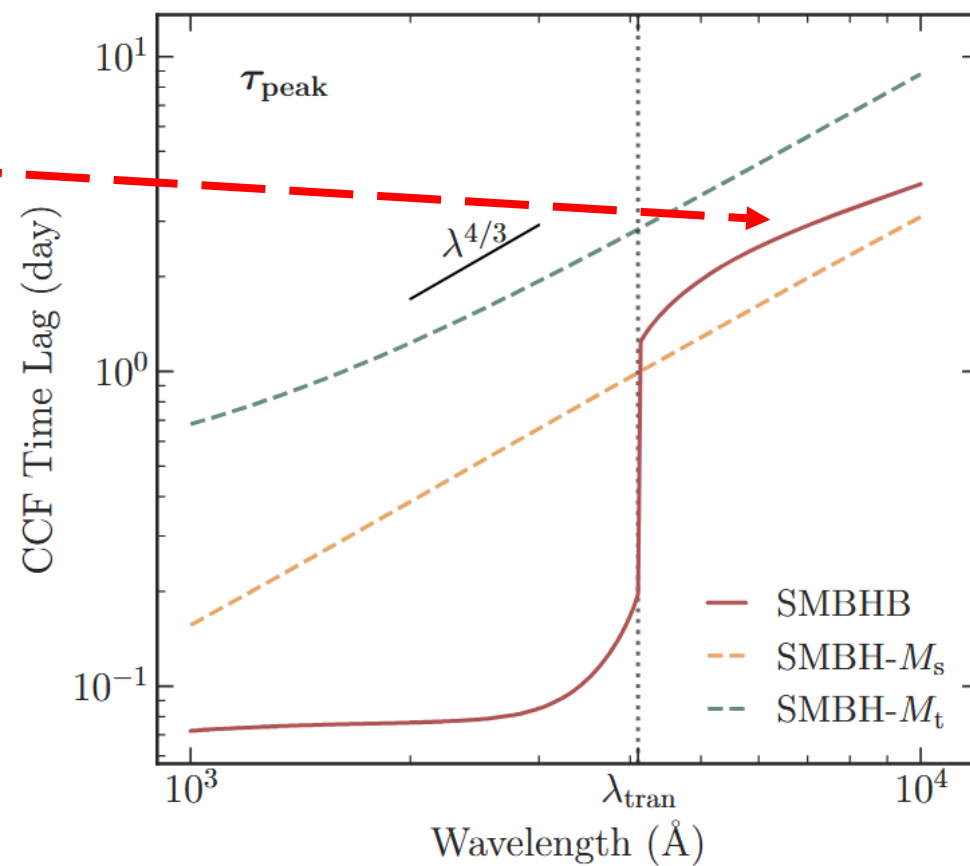
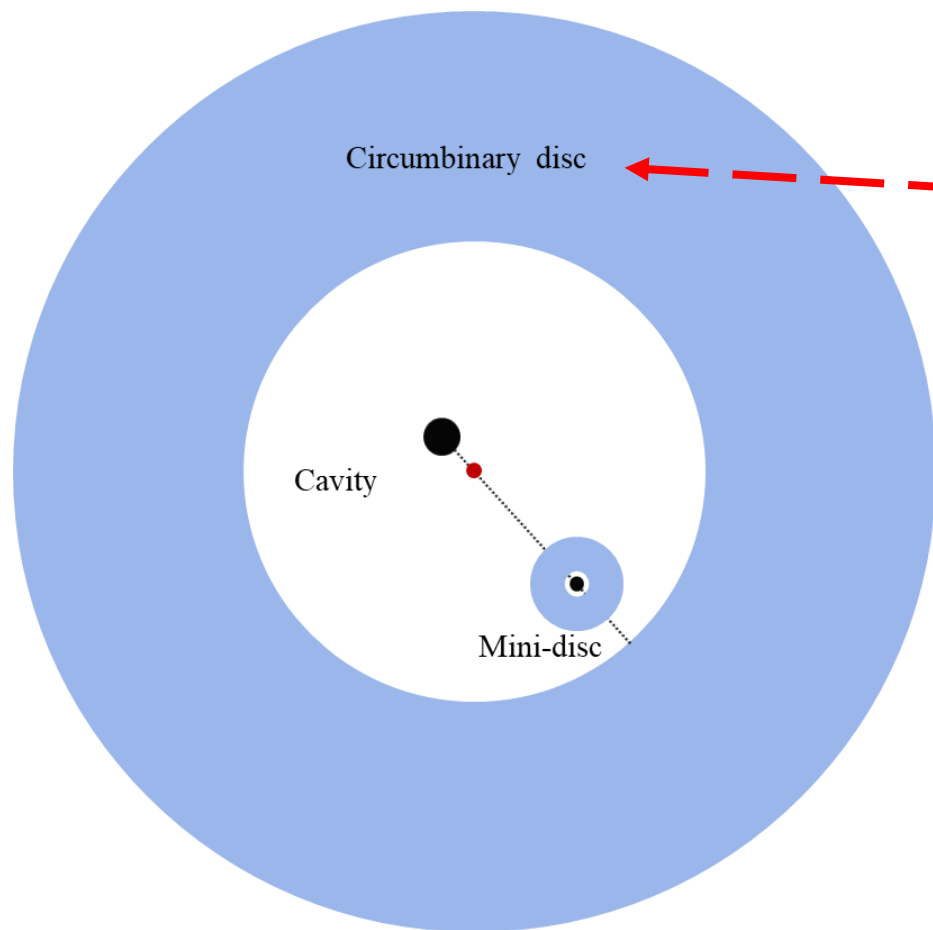
$$\tilde{\tau}_{\text{cent}} = \frac{\int_{>80\%} \tau \psi_{\otimes}(\lambda, \tau) d\tau}{\int_{>80\%} \psi_{\otimes}(\lambda, \tau) d\tau}$$



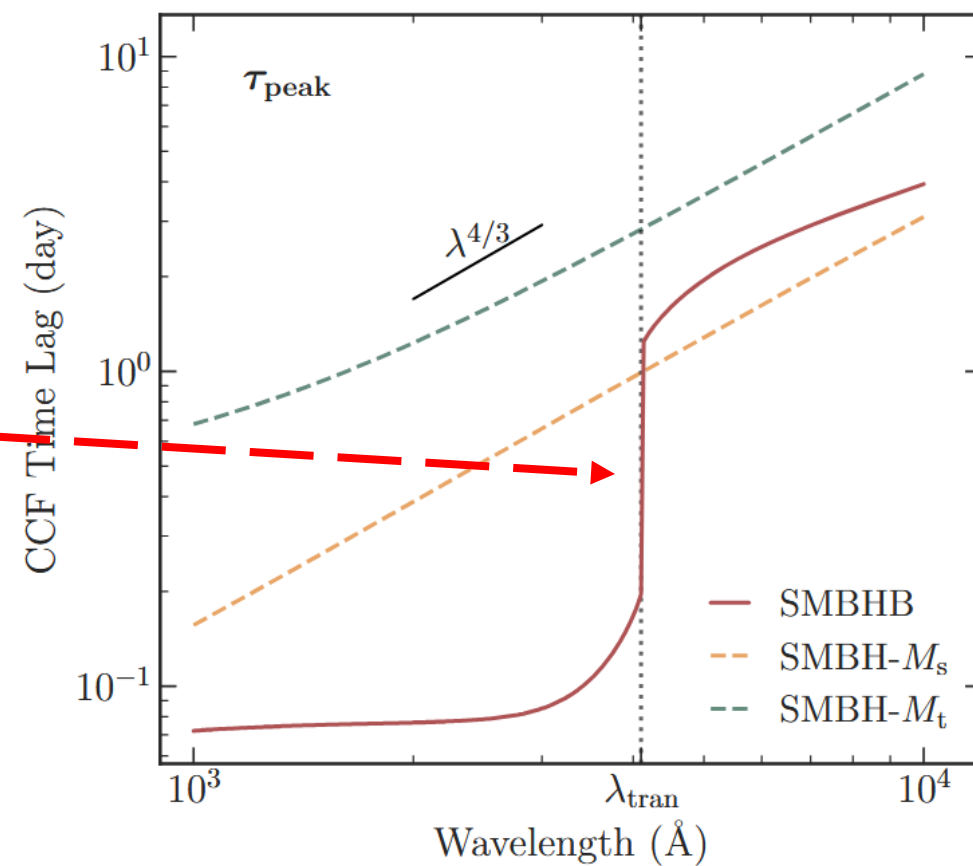
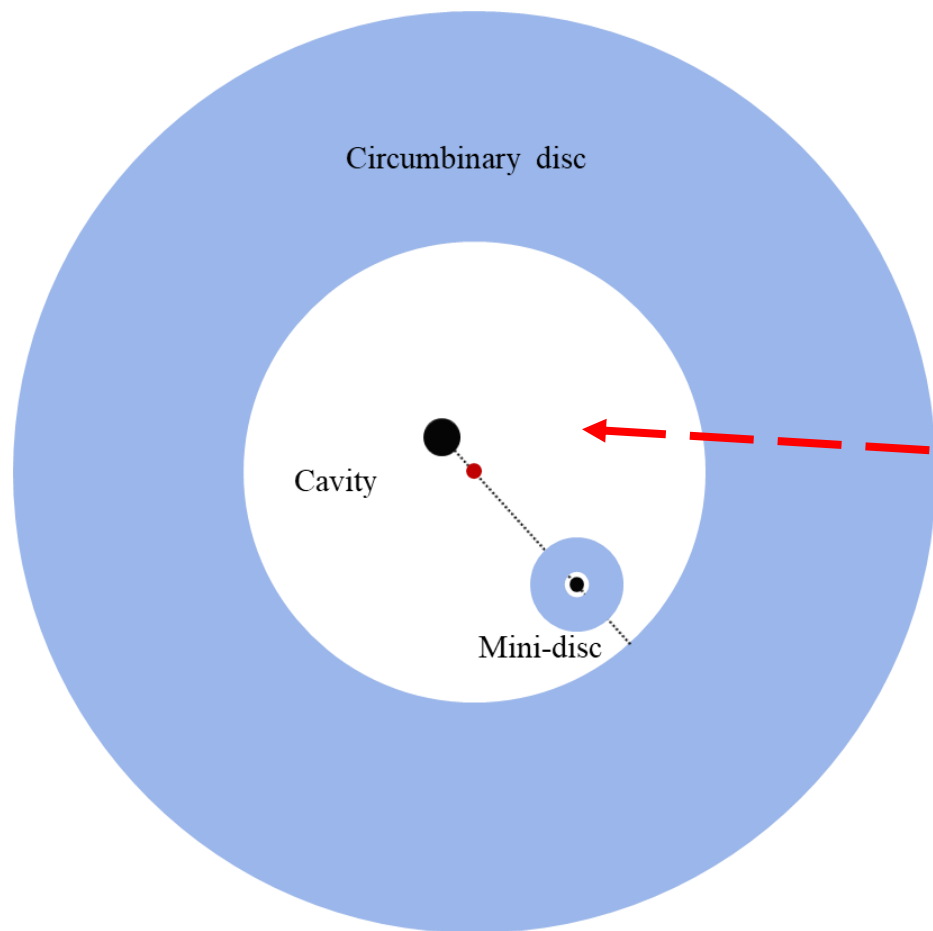
Low-mass-ratio SMBHBs: τ - λ relation



Low-mass-ratio SMBHBs: τ - λ relation



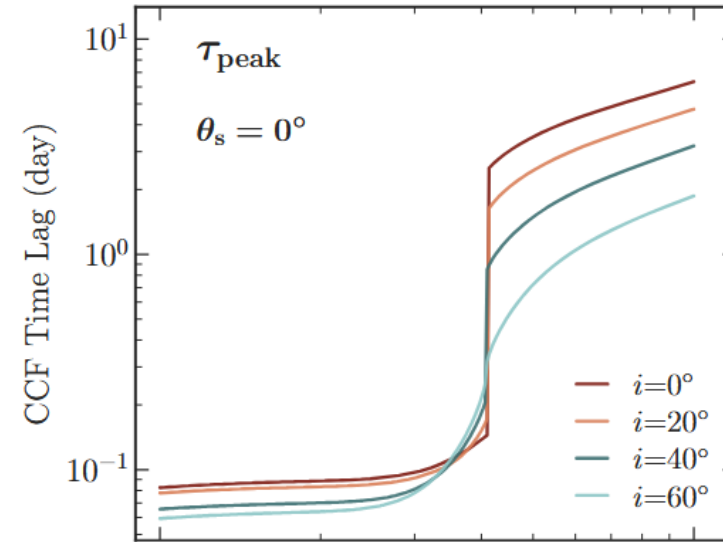
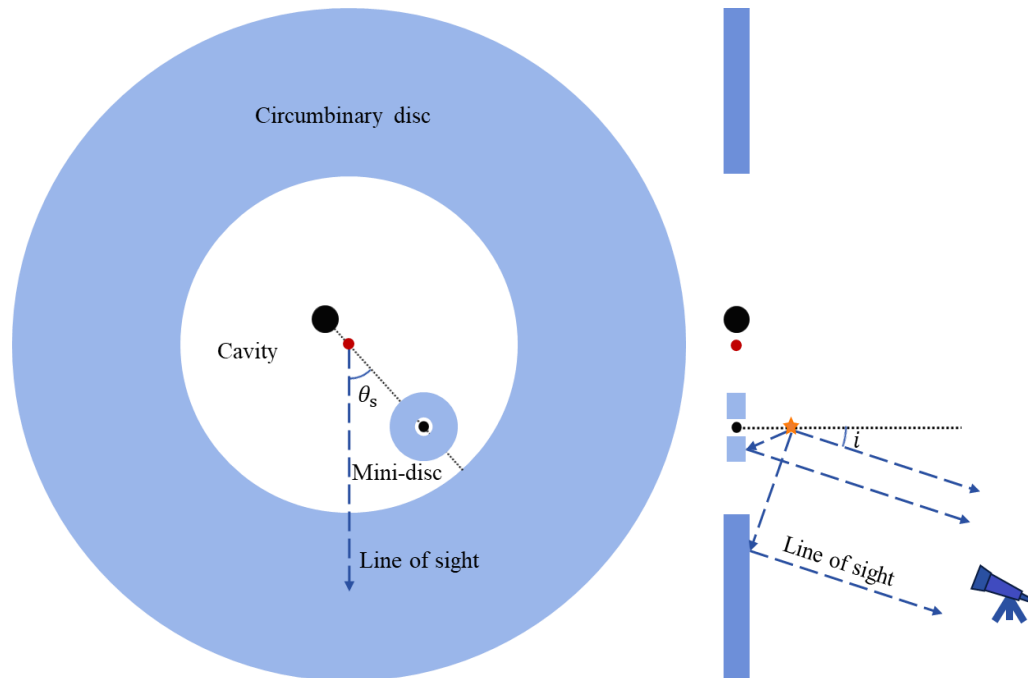
Low-mass-ratio SMBHBs: τ - λ relation



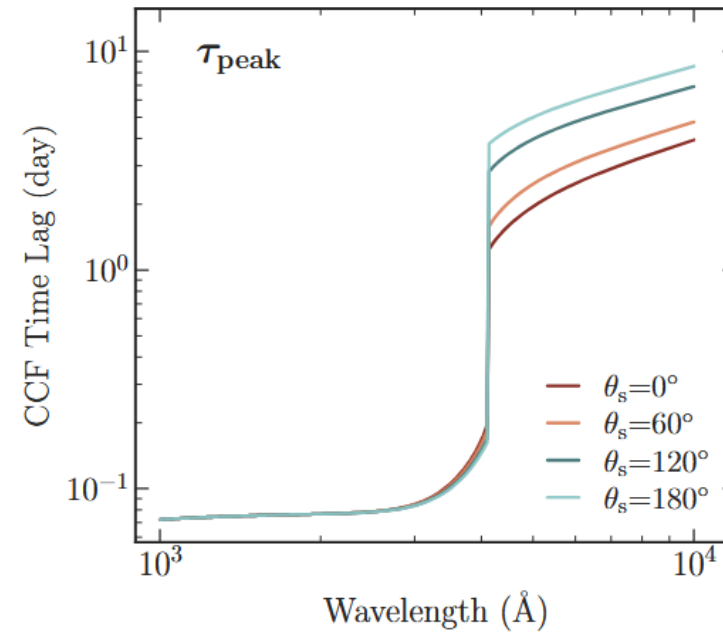
Low-mass-ratio SMBHBs: τ - λ relation

Inclination & orbital phase

- change relation shape
- mainly affect optical time lag
- τ - λ transition is retained



inclination

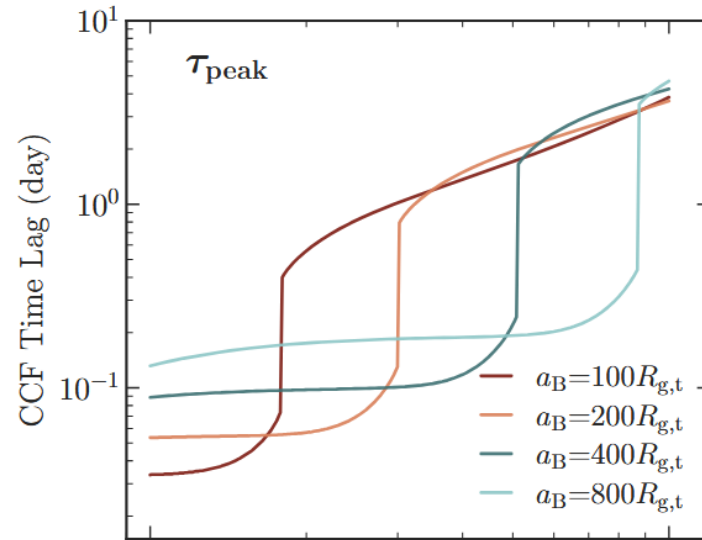
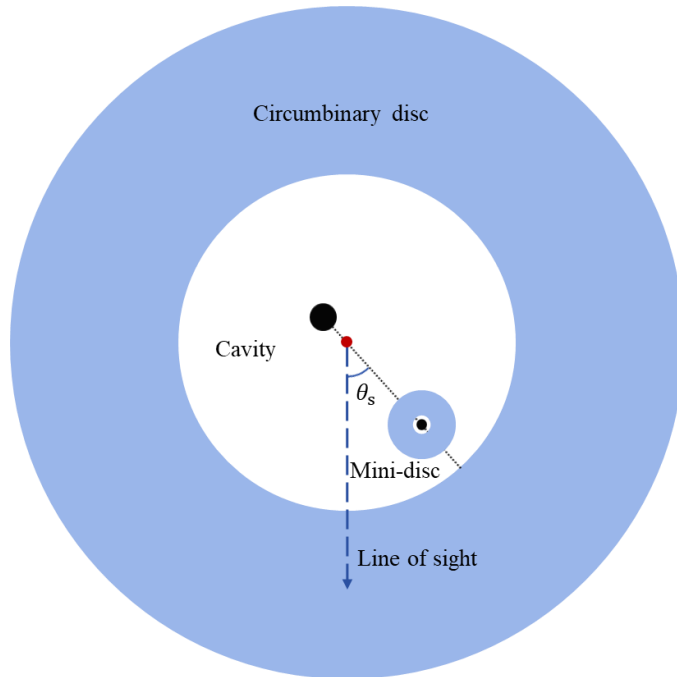


orbital phase

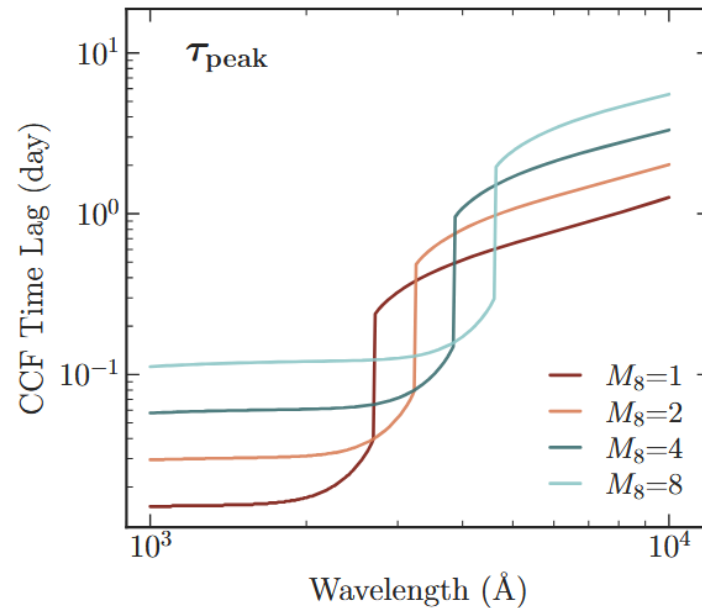
Low-mass-ratio SMBHBs: τ - λ relation

orbital separation & total mass

- change cavity size
- change transition wavelength

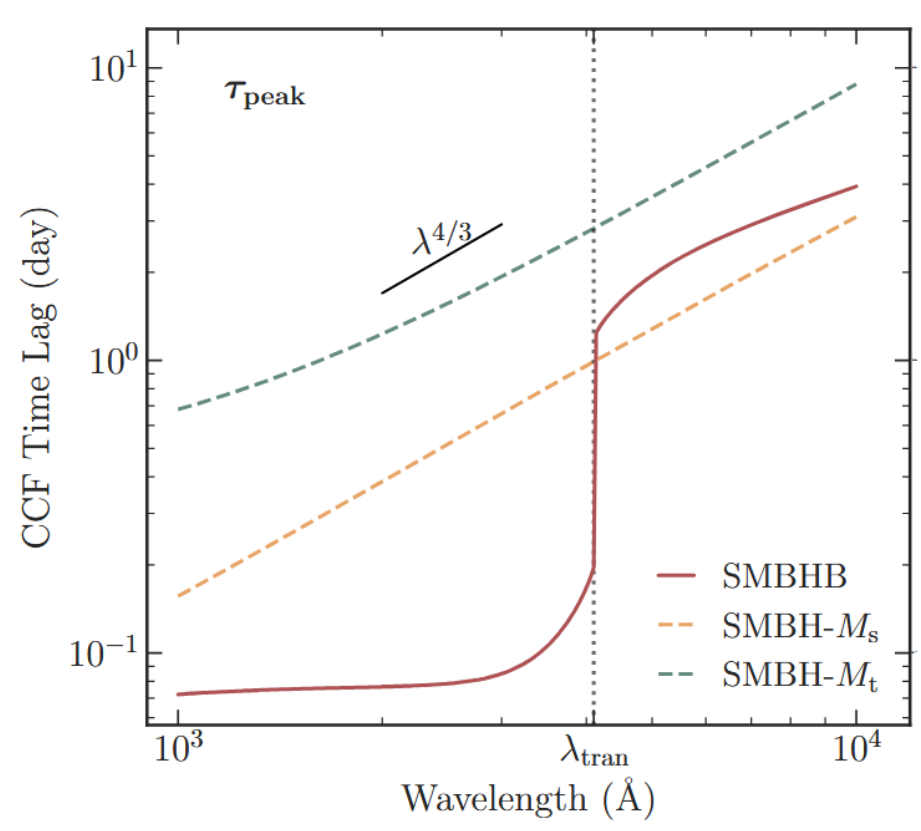


orbital separation



total mass

Low-mass ratio SMBHBs: τ - λ relation



$$\lambda_{\text{tran}} \approx 2700 f^{-1/4} \left(\frac{M_t}{10^8 M_\odot} \right)^{1/4} \left(\frac{\dot{m}_c}{0.1} \right)^{-1/4} \left(\frac{a_B}{100 R_{g,t}} \right)^{3/4} \text{\AA}$$

$$\approx 8600 f^{-1/4} \left(\frac{M_t}{10^8 M_\odot} \right)^{-1/4} \left(\frac{\dot{m}_c}{0.1} \right)^{-1/4} \left(\frac{P_B}{\text{yr}} \right)^{1/2} \text{\AA}$$

Application to PG 1302-102



Basic properties

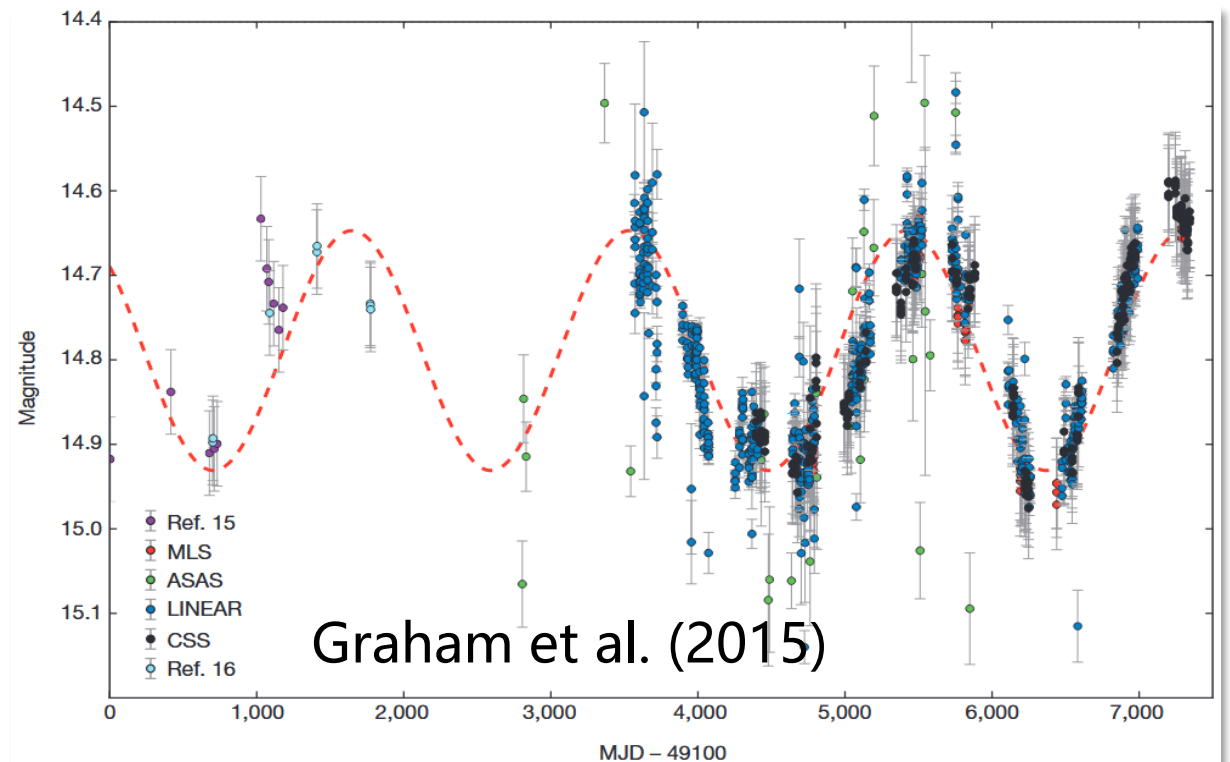
- Catalina Sky Survey
- Lincoln Near-Earth Asteroid Research
- $z = 0.2784$
- Magnitude $V = 15.0$
- Period **1884 days**

LETTER

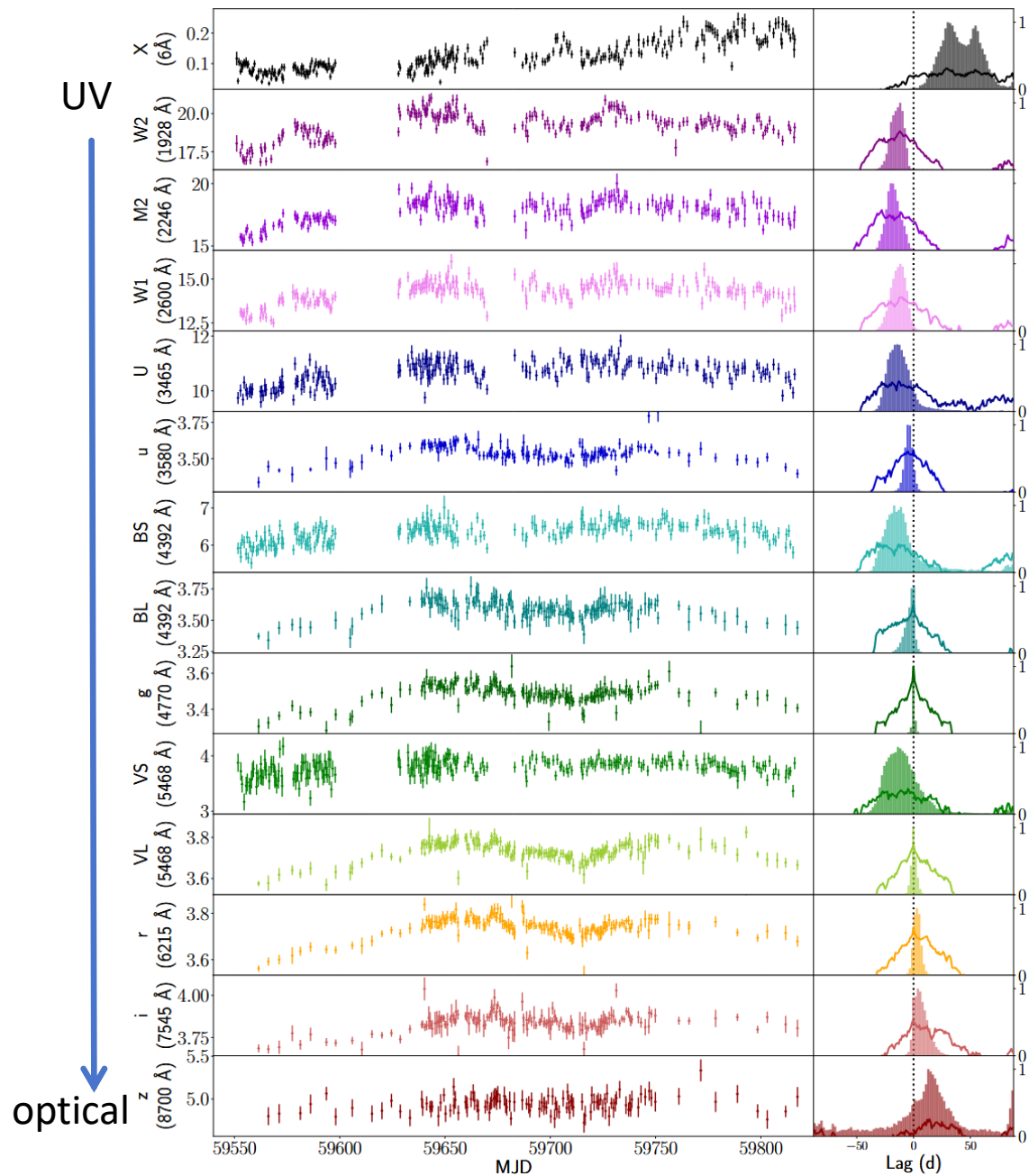
doi:10.1038/nature14143

A possible close supermassive black-hole binary in a quasar with optical periodicity

Matthew J. Graham¹, S. G. Djorgovski¹, Daniel Stern², Eilat Glikman³, Andrew J. Drake¹, Ashish A. Mahabal¹, Ciro Donalek¹, Steve Larson⁴ & Eric Christensen⁴



Graham et al. (2015)



THE ASTROPHYSICAL JOURNAL, 964:167 (8pp), 2024 April 1

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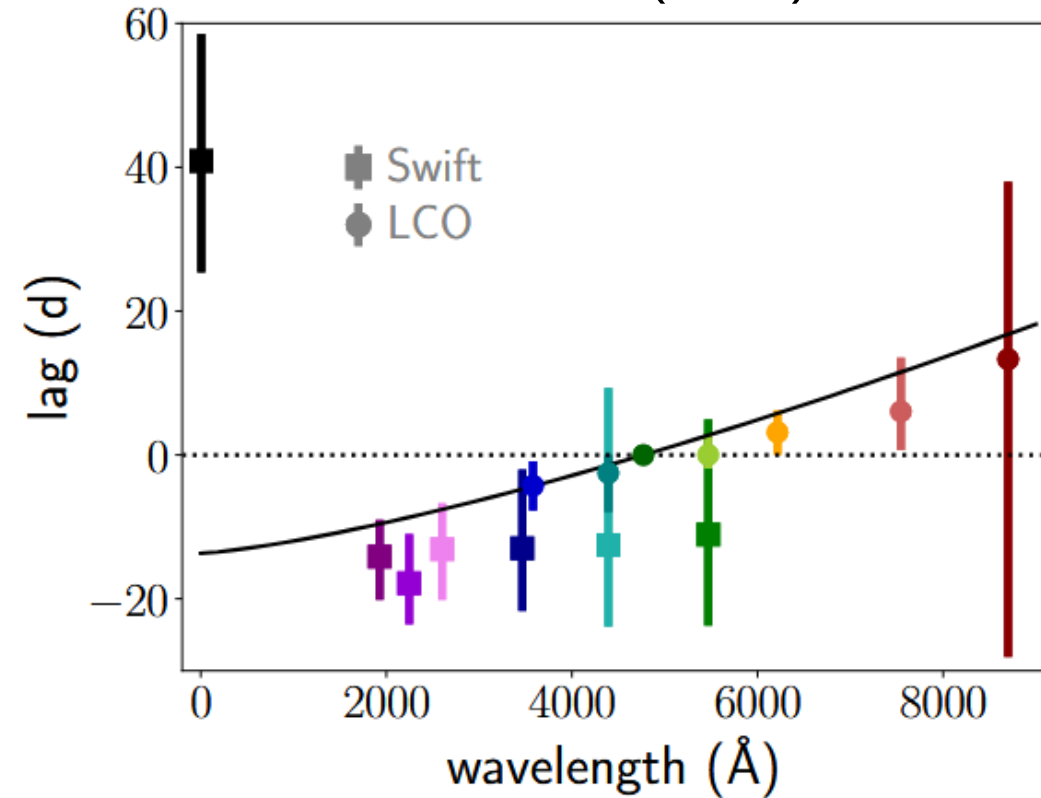
OPEN ACCESS

<https://doi.org/10.3847/1538-4357/ad23e2>

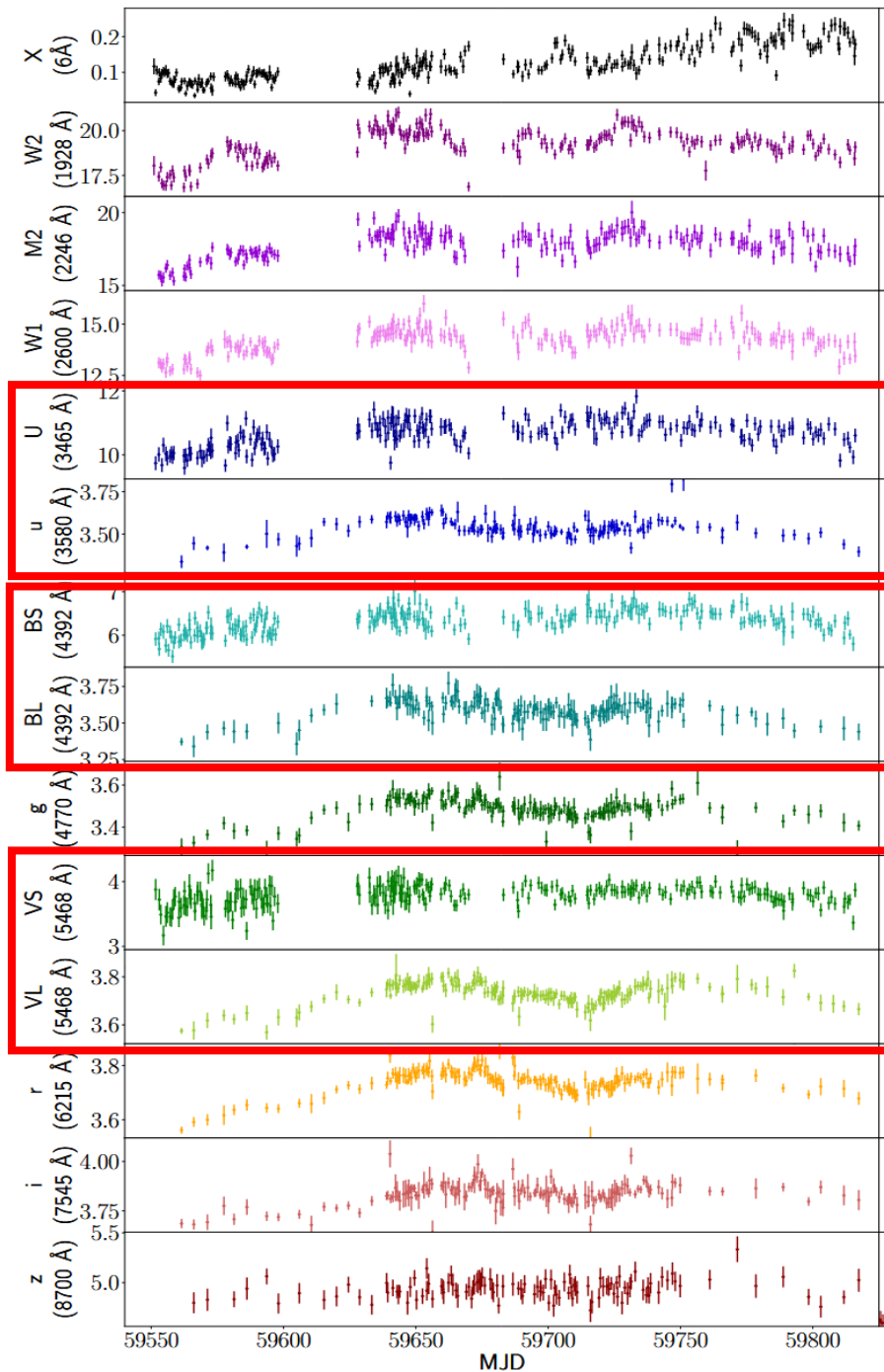


Intensive Swift and LCO Monitoring of PG 1302–102: Active Galactic Nucleus Disk Reverberation Mapping of a Supermassive Black Hole Binary Candidate

Liu et al. (2024)



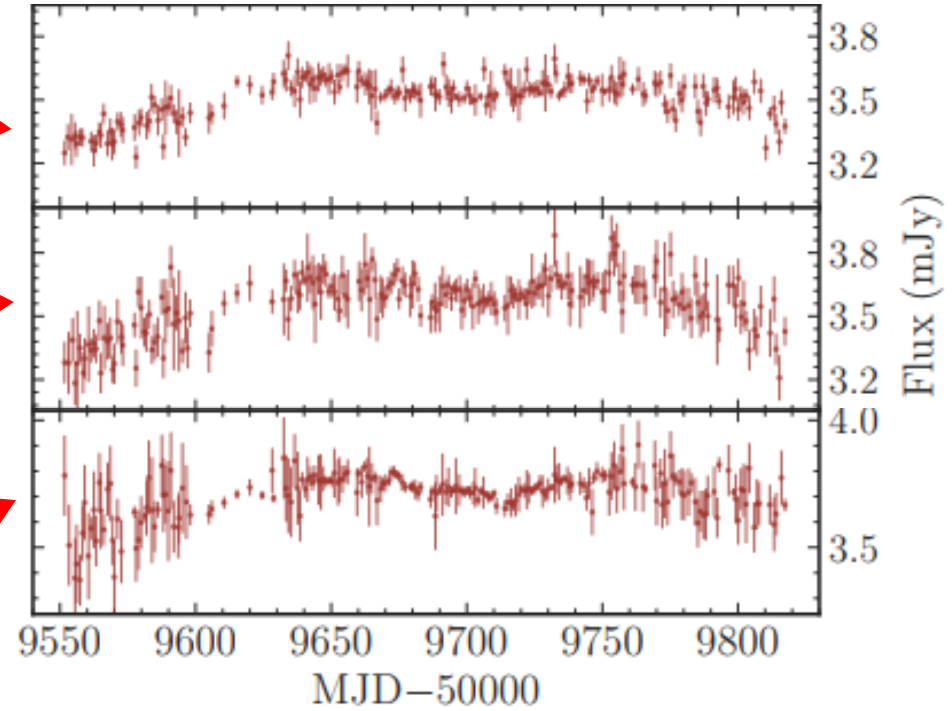
Light-curve combination



$u+U$

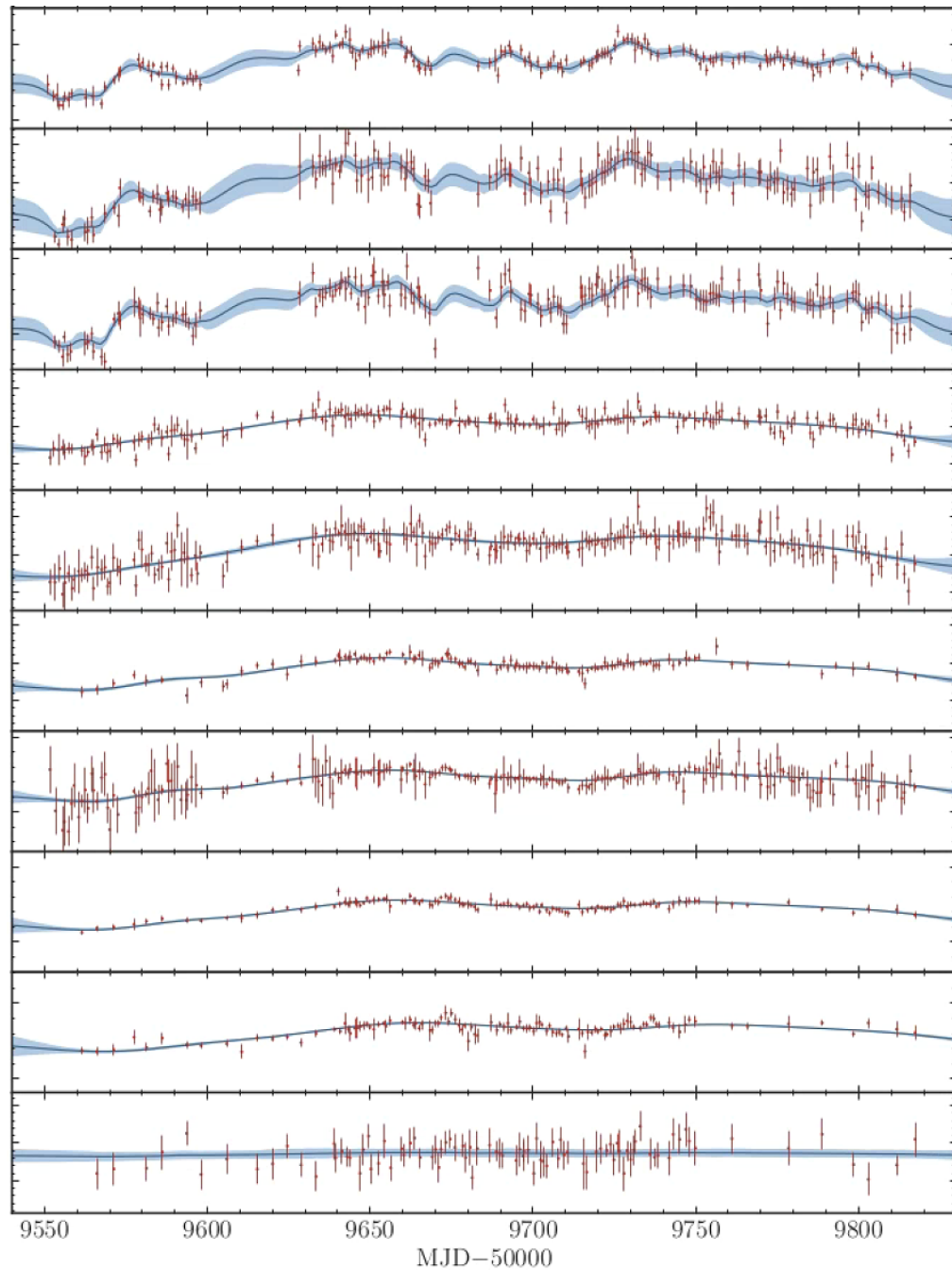
B

V



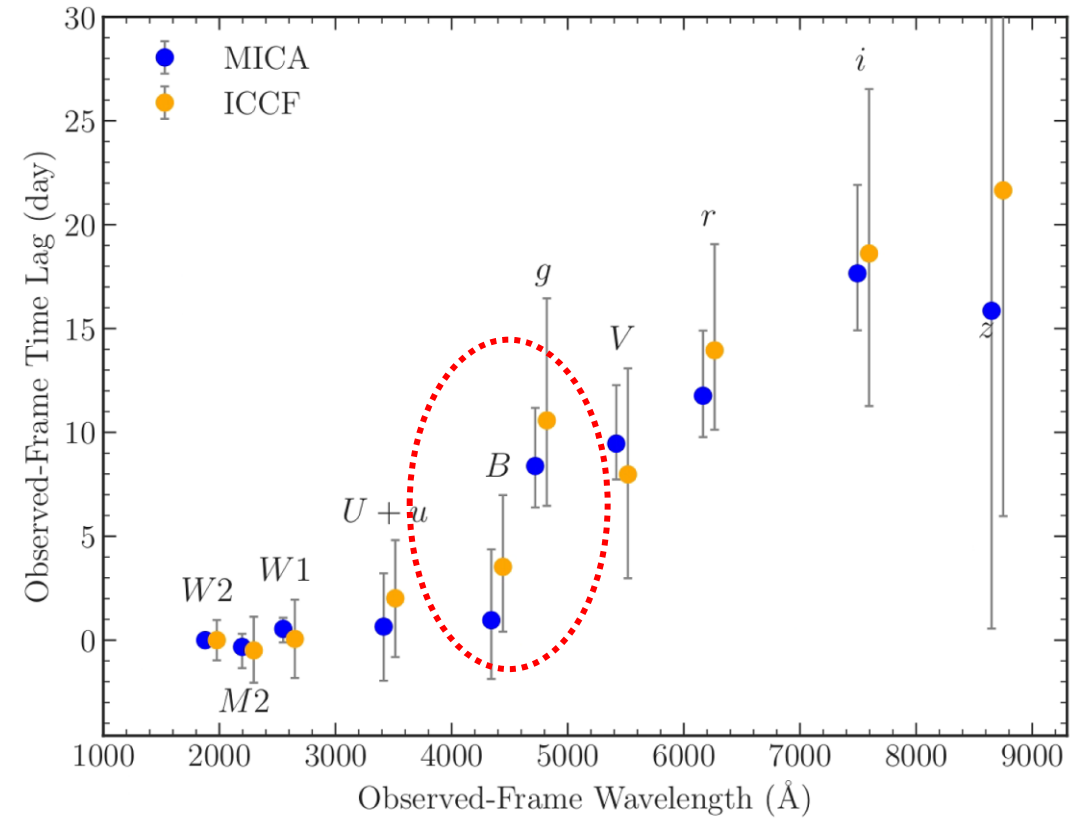
UV

optical

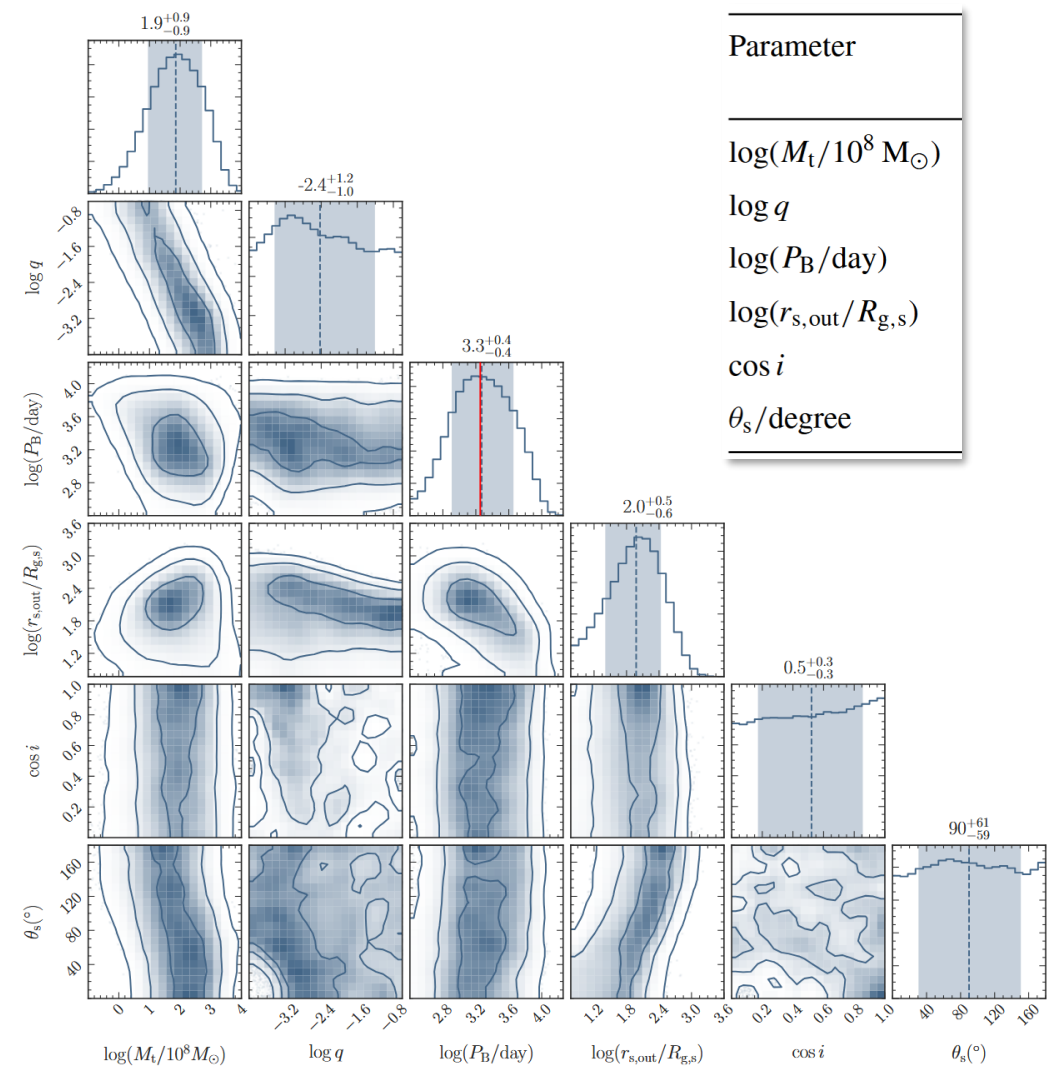
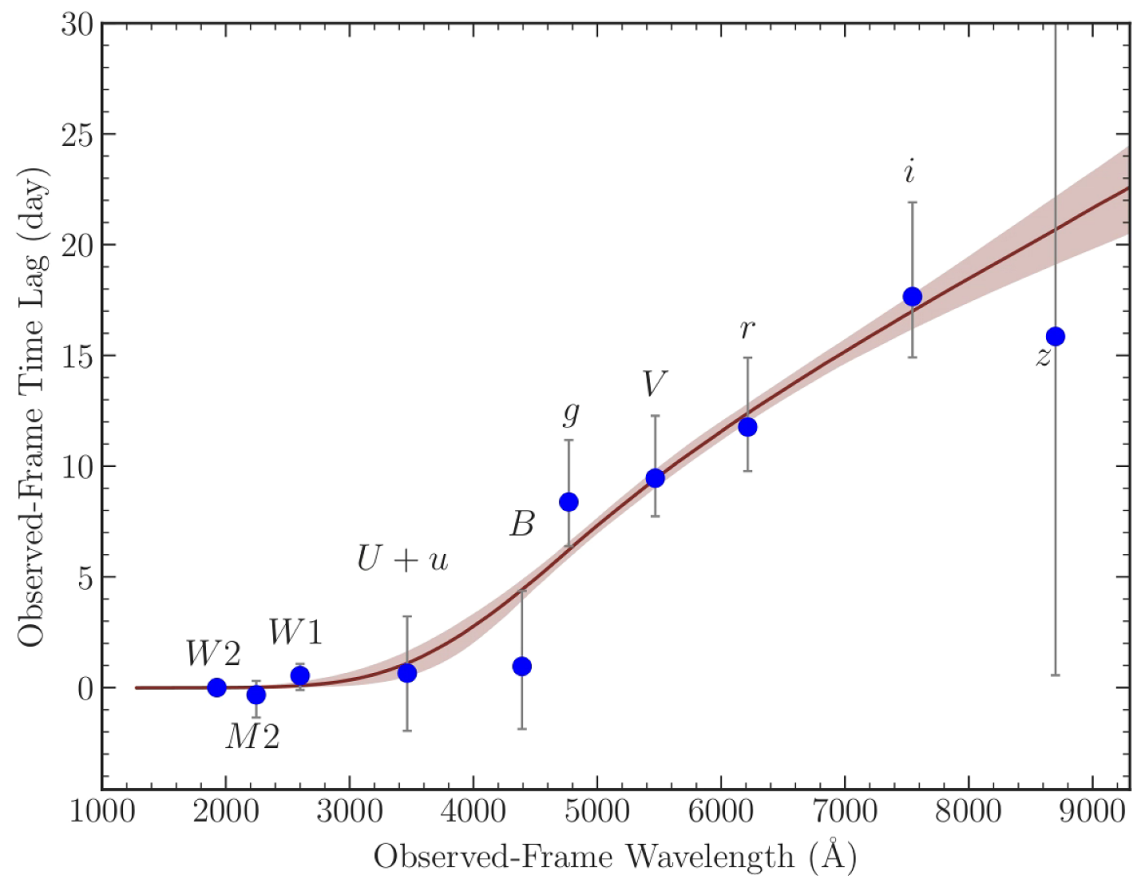


Time-lag measurement

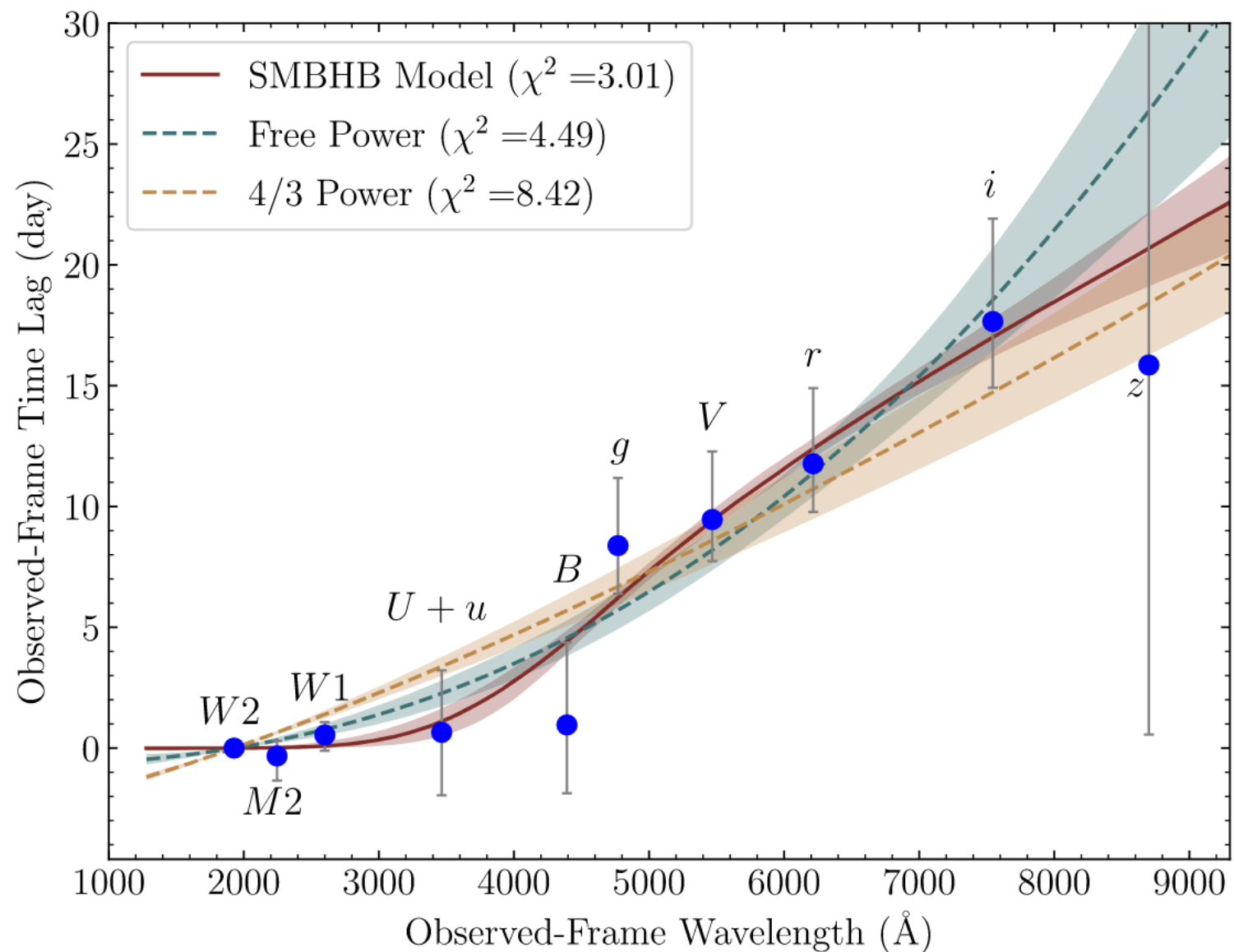
- ICCF
- MICA (with a Gaussian transfer function)



SMBHB model fits to time lag - wavelength relation

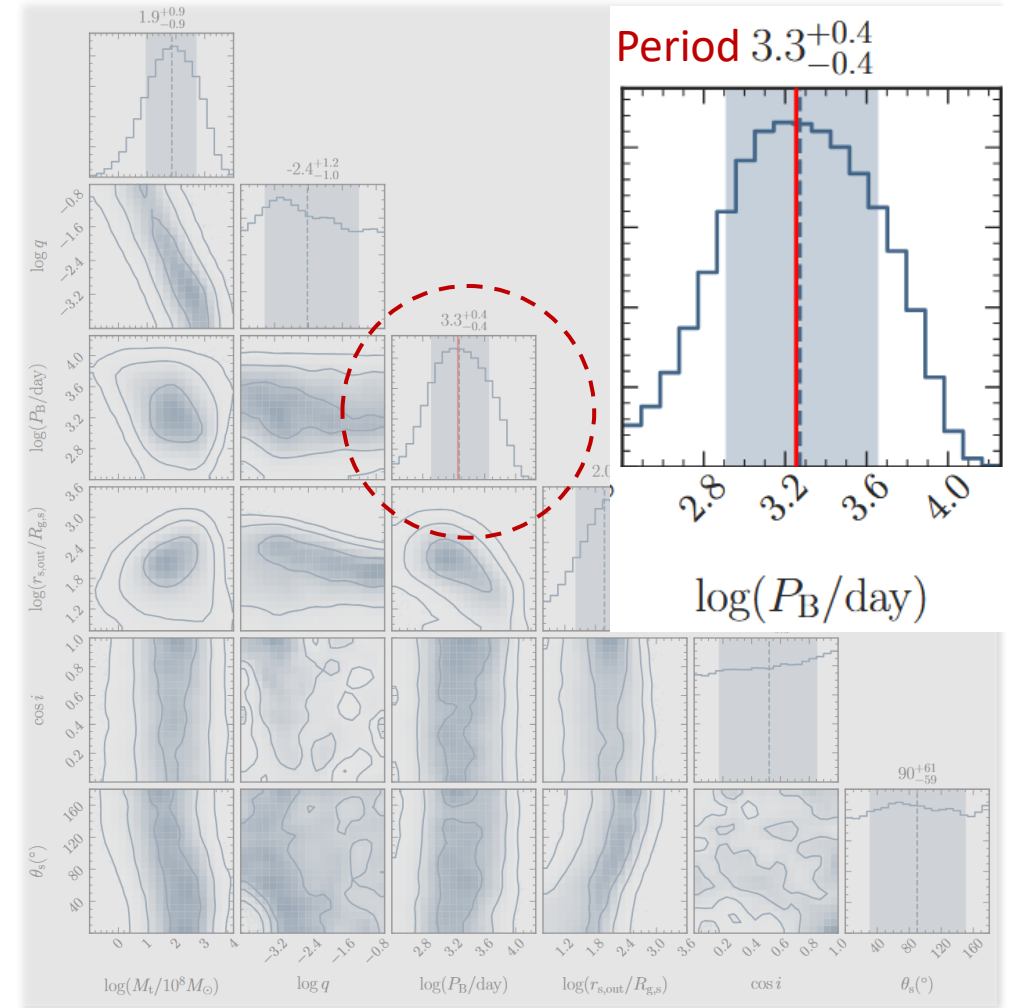
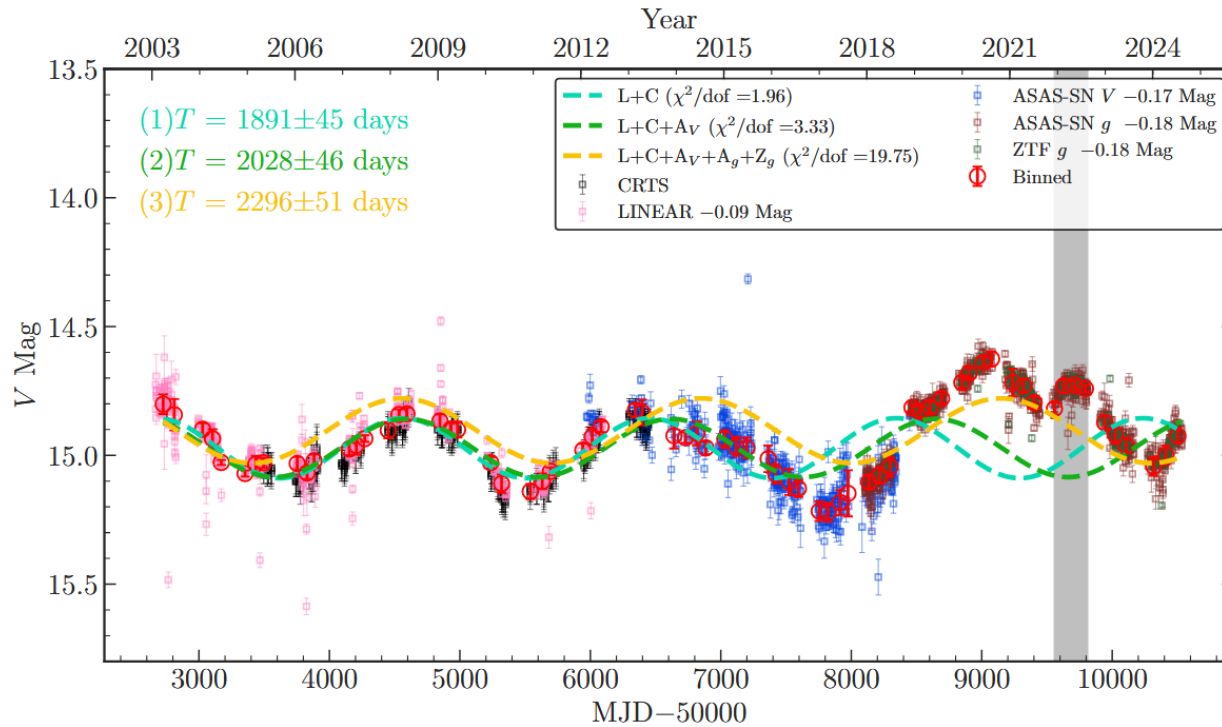


SMBHB model fits to time lag - wavelength relation

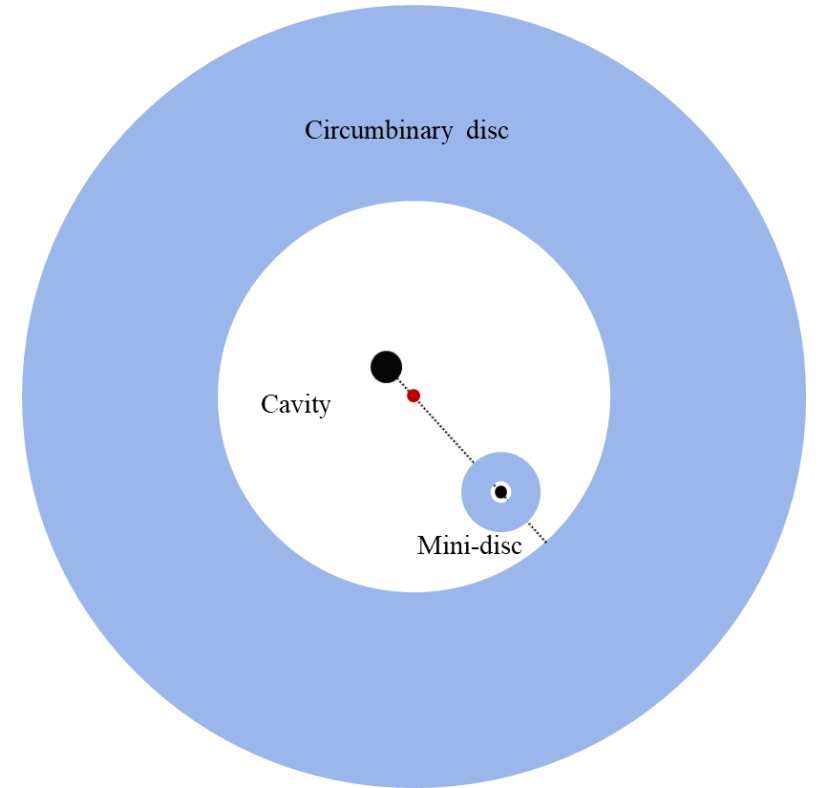
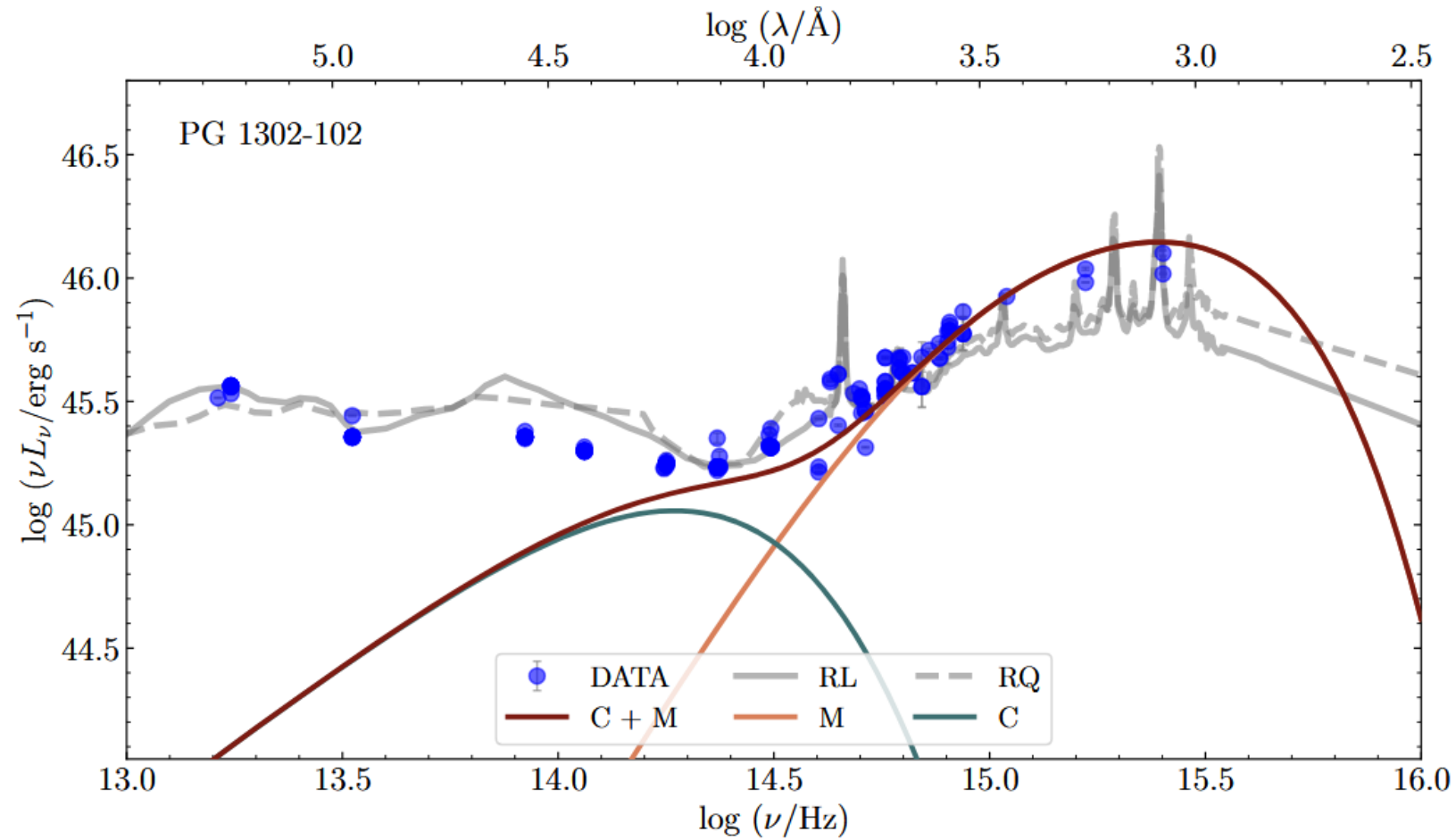


SMBHB model fits to time lag - wavelength reation

orbital period: $\log\left(\frac{P_B}{\text{day}}\right) = 3.3 \pm 0.4$ (~ 2000 days)



SMBHB model fits to time lag - wavelength relation

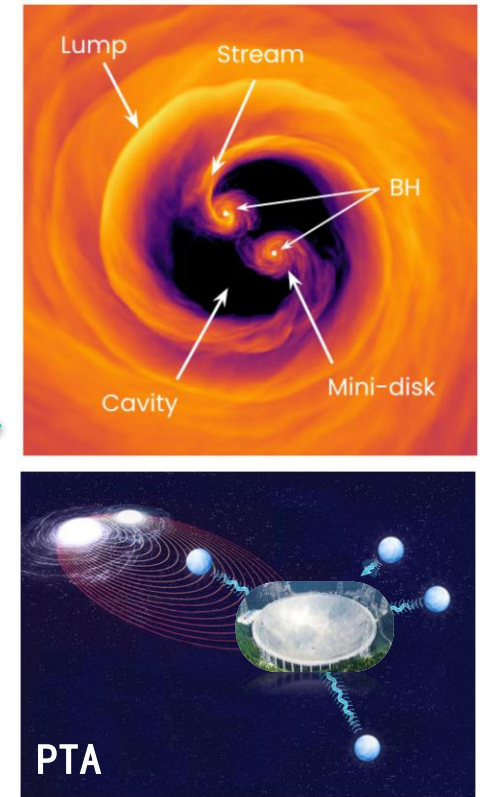
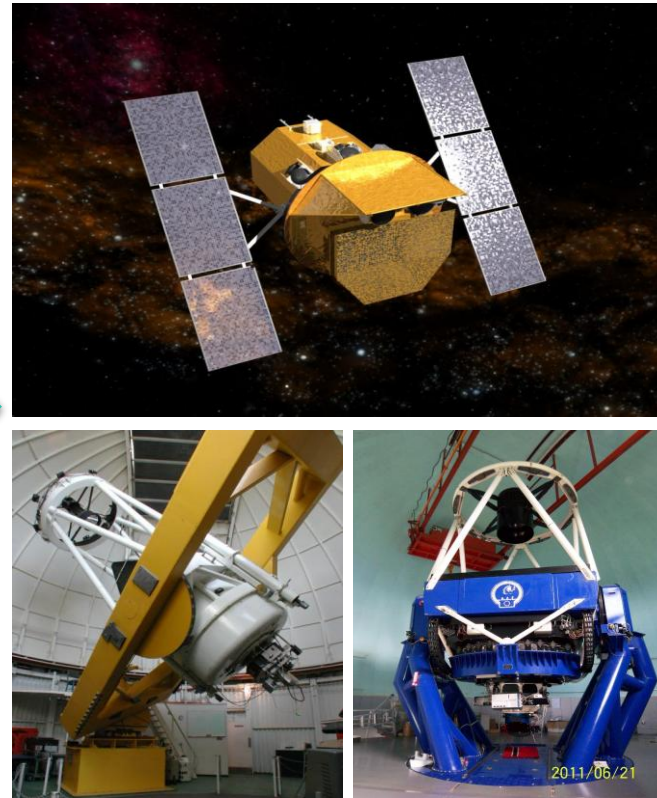
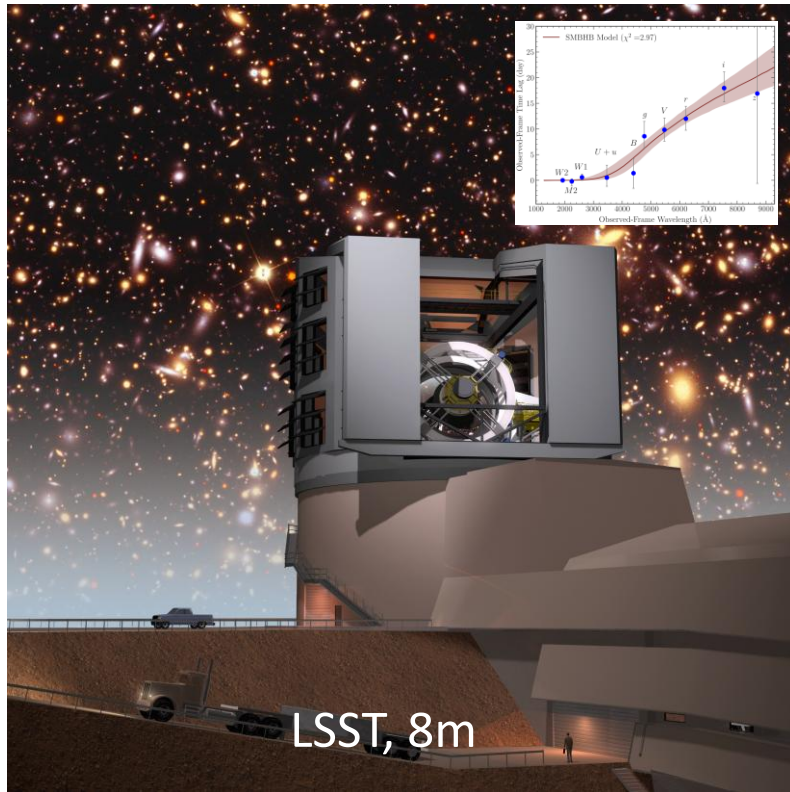


Future perspective

LSST 6 bands DDF: candidate sample

Dedicated observations

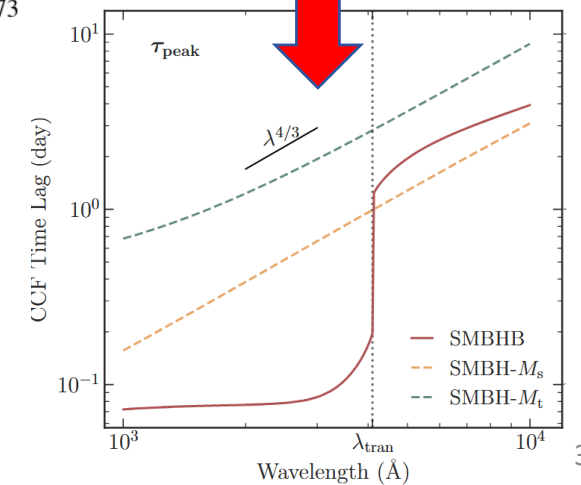
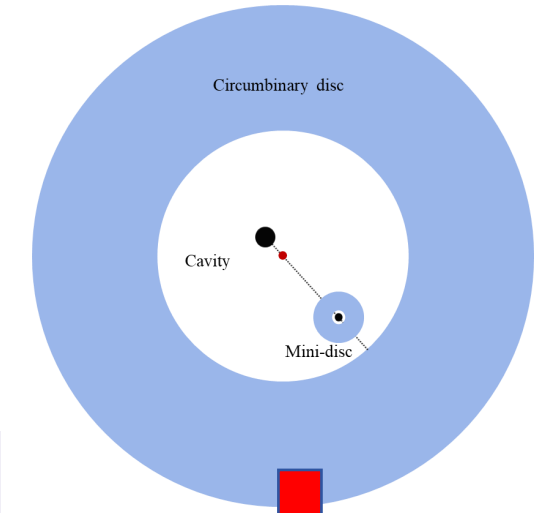
Synergy with PTA



Summary

- A new method for identifying SMBHBs: continuum reverberation mapping
- Application to PG 1302-102
- Future improvements:

Continuum RM signature when both BHs are active.



Monthly Notices
of the
ROYAL ASTRONOMICAL SOCIETY

MNRAS **543**, 2093–2115 (2025)
Advance Access publication 2025 September 04

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Continuum reverberation mapping of accretion discs surrounding supermassive black hole binaries: observational signatures

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