## NEW SOLUTION OF EARTH ORIENTATION PARAMETERS 1900-1992 FROM OPTICAL ASTROMETRY, AND ITS LINKING TO ICRF AND ITRF

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## Contents:

$\checkmark$ Introduction:

- Star catalog EOC-4 as a realization of ICRF;

↔Solution of Earth Orientation Parameters; - Linking the solution to ITRF;
$\checkmark$ Conclusions.

## Introduction (Catalog EOC-4):

- Between 1991 and 2003, we collected about 4.5 million optical observations of latitude / universal time / altitude variations at 33 observatories in 1899.7-2002.6;
- We recently combined these observations with astrometric catalogs ARIHIP (Wielen et al. 2001), Tycho-2 (Høg et al. 2000) and some other to derive EOC-4 (Vondrák \& Štefka, Astron. Astrophys. 2010):
- New approach assuring compatibility with Hipparcos/Tycho at their mean epoch (1991.25) and consequently to ICRF;
- EOC-4 contains 4418 different objects (stars, components of multiple systems, photocenters), out of which 599 have significant periodic motions.



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## Solution of EOP

$\checkmark$ Input data, based on observations of individual stars:

- Instantaneous latitude $\Delta \varphi$;
- Universal time UT0-UTC;
- Altitude differences $\delta \boldsymbol{h}$.
$\checkmark$ Solved parameters:
- At 5-day intervals:
$\star$ polar motion $x, y$, Universal time UT1- UTC (only after 1956);
- For each instrument:
* constant, linear, semi-annual and annual deviation in latitude/longitude ( $d e v_{\varphi}, d e v_{\lambda}$ ), and rheological parameter $\Lambda=1+k-l$;
- For the whole interval:
$\star$ celestial pole offsets $d X, d Y$ wrt IAU2000 nutation and IAU2006 precession, as quadratic function of time.


## Observations used:

- Data from 47 instruments at 33 observatories:
- 10 PZT's ( $\varphi$, UT0):
* 3 at Washington; 2 at Richmond and Mizusawa; 1 at Mount Stromlo, Punta Indio \& Ondřejov;
- 7 photoelectric transit instruments (only UT0): ※ 3 at Pulkovo; 1 at Irkutsk, Kharkov, Nikolaev \& Wuhang;
- 16 visual zenith-telescopes \& similar instruments (only $\varphi$ ):
* 7 ZT at ILS stations; 2 ZT at Poltava, 1 ZT at Belgrade, Blagoveschtchensk, Irkutsk, Jósefoslaw \& Pulkovo; FZT at Mizusawa; VZT at Tuorla-Turku;
- 14 instruments for equal altitude observations - AST, PAST, CZ ( $\delta h$ ):
* 1 AST at Paris, Santiago de Chile, Shanghai, Simeiz \& Wuhang; 2 PAST at Shaanxi, 1 PAST at Beijing, Grasse, Shanghai \& Yunnan; 1 CZ at Bratislava, Prague \& Ondřejov.


## Geographic distribution of participating observatories



## Simplified observation equations:

$\Delta \varphi=x \cos \lambda-y \sin \lambda-d X \cos \alpha-d Y \sin \alpha+d e \nu_{\varphi}+\Lambda D_{\varphi}$
$15 \cos \varphi(\mathrm{UT} 0-\mathrm{UTC})=15 \cos \varphi(\mathrm{UT} 1-\mathrm{UTC})+\sin \varphi(x \sin \lambda+y \cos \lambda)+$
$+\cos \varphi \tan \delta(d Y \cos \alpha-d X \sin \alpha)+d e v_{U T}+15 \Lambda D_{\lambda} \cos \varphi$
$d h=15 \cos \varphi \sin a(\mathrm{UT} 1-\mathrm{UTC})+x(\cos \lambda \cos a+\sin \varphi \sin \lambda \sin a)-$
$-y(\sin \lambda \cos a-\sin \varphi \cos \lambda \sin a)+d Y(\sin q \sin \delta \cos \alpha-\cos q \sin \alpha)-$
$-d X(\sin q \sin \delta \sin \alpha+\cos q \cos \alpha)+d e v_{\varphi} \cos a+d e v_{U T} \sin a+$
$+\Lambda\left(D_{\varphi} \cos a+15 D_{\lambda} \cos \varphi \sin a\right)$,
$\varphi, \lambda$ are geographic coordinates of the instrument,
$\alpha, \delta, a, q$ are right ascension, declination, azimuth, parallactic angle,
$D_{\varphi}, D_{\lambda}$ are rigid Earth tidal variations of the local vertical.

## $\checkmark$ Celestial reference frame is realized by EOC-4;

- More strict criteria to exclude outliers:
\gg0.7" (instead of 0.8") for deviations from monthly average;
> $\mathbf{2} .5 \sigma_{0}$ (instead of $2.7 \sigma_{0}$ ) for residuals;
- Thus, 2.7\% of observations were excluded;
- $\sigma_{0}=0.184^{\prime \prime}$ (instead of 0.190");
$\checkmark$ Terrestrial reference frame is realized by adopting geographic coordinates of the stations and correcting the observations for the motions from NUVEL-1A.
- We also expect that coordinates of each station can have apparent seasonal deviations due to refraction anomalies.

For each station, we estimate systematic deviations in latitude/universal time in the form:

$$
d e v_{\varphi, U T}=A^{\varphi, U T}+A_{1}^{\varphi, U T} T+B^{\varphi, U T} \sin 2 \pi t+C^{\varphi, U T} \cos 2 \pi t+D^{\varphi, U T} \sin 4 \pi t+E^{\varphi, U T} \cos 4 \pi t,
$$

where $T$ is measured in Julian centuries from MJD $=32000$ (latitude) and 43000 (for UT), $t$ in years from the beginning of Besselian year. These 12 parameters are tied by the following 18 constraints ( $\lambda$ is the longitude of the station)

$$
\begin{aligned}
\sum p A^{\varphi}\left\{\begin{array}{l}
\sin \lambda \\
\cos \lambda
\end{array}\right\}=\sum q A_{1}^{\varphi}\left\{\begin{array}{l}
\sin \lambda \\
\cos \lambda
\end{array}\right\}=\sum p B^{\varphi}\left\{\begin{array}{l}
\sin \lambda \\
\cos \lambda
\end{array}\right\} & =\sum p C^{\varphi}\left\{\begin{array}{l}
\sin \lambda \\
\cos \lambda
\end{array}\right\}= \\
& =\sum p D^{\varphi}\left\{\begin{array}{l}
\sin \lambda \\
\cos \lambda
\end{array}\right\}=\sum p E^{\varphi}\left\{\begin{array}{l}
\sin \lambda \\
\cos \lambda
\end{array}\right\}=0,
\end{aligned}
$$

$$
\sum p A^{U T}=\sum q A_{1}^{U T}=\sum p B^{U T}=\sum p C^{U T}=\sum p D^{U T}=\sum p E^{U T}=0
$$

In all our previous solutions, we applied the summations to the stations that finished observations after 1962, with weights proportional to the length of the interval covered by observations $(p)$ and its third power $(q)$. So, e.g., the trend of the polar motion of our solution is given as a weighted mean of $A_{1}{ }^{\varphi}$ of all stations in latitude, projected into $x, y$ axes.
trends in latitude


## Comparison with space techniques (solution IERS C04):

- Linear trend of the solution is fixed to the most stable stations, as explained above;
- Bias and seasonal effects are estimated from the differences of pole coordinates $x, y$ and UT between IERS C04 and our optical astrometry solution. Only the data after 1978 (when space techniques became dominant) are used.


## Differences C04-OA09 - polar motion



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## Differences C04-OA09 - Universal time



## Polar motion ["]:



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## Length-of-day, computed from UT1-TAI [seconds]:



Celestial pole offsets:

$$
\begin{aligned}
d X= & -7.4+29.0 T+29.0 T^{2}[\mathrm{mas}] \\
d Y= & -6.1+8.9 T-1.2 T^{2}[\mathrm{mas}] \quad T \text { in centuries from } 1956.0 \\
& \pm 0.4 \quad 1.1 \quad 3.4
\end{aligned}
$$

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Rheological parameter $\Lambda=1+\boldsymbol{k}-\boldsymbol{l}$


## Conclusions:

- 4505442 individual observations, based on catalog EOC-4, were used in the new solution covering the interval 1899.7-1992.0;
-Solution is linked to terrestrial reference frame via the solution by space techniques (bias + seasonal terms, 1978.0-1992.0), and via the most stable stations corrected for NUVEL-1A motions (trend, 1899.7-1992.0);
$\diamond$ New solution yields slightly better results than the ones based on previous versions of EOC:
- The average standard error of one observation is $\sigma_{0}=0.184^{\prime \prime}$ (former value = 0.190").

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