## MORE ACCURATE FOCAL LENGTH DETERMI NATION FOR THE ROZHEN 2-m TELESCOPE

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## INTRODUCTI ON

The focal length of a telescope is an important parameter in determining the relative coordinates (angular separation and positional angle) of double and multiple stars, as well as in determining the precise coordinates of radio sources that are visible in optical part of wavelengths. With the $2-m$ telescope of NAO Rozhen we have collected a large number of observations of these objects. In order to determine the focal length more accurately we have used CCD images obtained at Rozhen.

## THE ROZHEN 2-m TELESCOPE

## Ritchey-Chretien-Coude (RCC) Telescope



## OPTICAL DESIGN



1 - $2 m$ primary hyperbolic mirror
2a - RC secondary hyperbolic mirror
$F^{\prime}$ - Ritchey-Chretien focus

By system Ritchey-Chretien:
Focal lenght - 16 m;
Focal ratio - F/8.

## CCD-Camera VersArray: 1300 B



Sponsored by UNESCO - ROSTE
$1340 \times 1300$ active pixels, $20 \times 20 \mu \mathrm{~m}$ pixel size
The pixel size is 0.26 arcseconds
Cooling temperature $-110^{\circ} \mathrm{C}$, liquid nitrogen

## OBSERVATIONS

$\square \quad$ Our team has performed 8 series of CCD observations of visual double and multiple stars at the NAO Rozhen in the period from 2004 to 2012. Also, we have performed 3 series of CCD observations of extragalactic compact radio sources (ERS) that are visible at optical wavelengths in order to investigate the relation between the optical and radio reference frames.

ㅁ The first series - in the middle of October 2004 (the frames were obtained by using the Photometrics AT200 CCD camera)
$\square \quad$ The other 7 series of CCD observations of visual double and multiple stars:

- in the end of October 2005;
- on December 16/17, 2006;
- on July 20/21, 2009;
- on September 7-10, 2010;
- from March 29 to April 01, 2011;
- on October 27-28, 2011 and
- on April 24-26, 2012.


## OBSERVATIONS

$\square$ In the last seven series the frames were obtained by using the CCD camera VersArray: 1300B.

- A total of 891 pairs were measured
- The 3 series of CCD observations of ERS :
- from March 29 to April 01, 2011;
- on October 27-28, 2011 and
- on April 24-26, 2012.
- About 100 ERS objects were measured


WDS $00057+4549=$ STT 547


WDS $00159+5233=E S 865$


WDS $00152+2722=\mathrm{J} 868$


ERS L 2254+074

$$
y=0.0019+0.0137 x
$$



| NAOR | ASV | diff. |
| ---: | ---: | ---: |
| 44.61 | 45.23 | 0.62 |
| 62.90 | 63.76 | 0.86 |
| 107.41 | 108.86 | 1.45 |
| 109.72 | 111.26 | 1.54 |
| 115.45 | 117.03 | 1.58 |
| 120.59 | 122.21 | 1.63 |
| 142.43 | 144.39 | 1.97 |
| 148.39 | 150.47 | 2.08 |
| 155.05 | 157.17 | 2.13 |
| 189.11 | 191.69 | 2.58 |

## FOCAL LENGTH

The telescope focal length is an important parameter in determining the angular pixel size. It is used for the purpose of determining the relative coordinates (angular separation and positional angle) of double and multiple stars, as well as in determining the precise coordinates of radio sources.
The effective focal length $F$ for a two-mirror system is given by (Bely 2003):


$$
F=\frac{f_{1} f_{2}}{f_{1}+f_{2}-s}
$$

Scheme of a two-mirror system: $\mathrm{f1}$ is the primary mirror focus, f 2 is the effective focus and s is the distance between the two mirrors

## CALCULATI ON AND RESULTS

The angular separation $d_{c}$ between two objects (arc along a great circle of celestial sphere) is calculated from coordinates $\alpha_{i}$ and $\delta_{i}, i=1,2$ for the epoch of observations according to the formula

$$
\cos d_{c}=\sin \delta_{1} \sin \delta_{2}+\cos \delta_{1} \cos \delta_{2} \cos \left(\alpha_{2}-\alpha_{1}\right)
$$

The measured separation $d_{m}$ is calculated from

$$
d_{m}=\frac{3600 \times 180}{\pi} \sqrt{\left(x_{1}-x_{2}\right)^{2}+\left(y_{1}-y_{2}\right)^{2}},
$$

The telescope focal length is obtained from

$$
F=\frac{d_{m}}{d_{c}}
$$

Table 1. Focal length of 2 m telescope at NAO Rozhen with attached CCD camera VersArray 1300B.

| pairs | $\begin{aligned} & \hline n_{1} \\ & {\left[{ }^{o}\right]} \end{aligned}$ | $\begin{aligned} & \dot{\delta}_{1} \\ & {\left[{ }^{\circ}\right]} \end{aligned}$ | $\mu_{\alpha_{1}} \cos \delta_{1}$ $[\mathrm{mas} / \mathrm{yr}]$ | $\begin{gathered} \mu_{\delta_{1}} \\ {[\mathrm{mas} / \mathrm{yr}]} \end{gathered}$ | $\begin{aligned} & \alpha_{2} \\ & {[o]} \end{aligned}$ | $\begin{aligned} & \hline \delta_{2} \\ & {[0]} \end{aligned}$ | $\begin{gathered} \mu_{\alpha_{2}} \cos \delta_{2} \\ {[\mathrm{mas} / \mathrm{yr}]} \end{gathered}$ | $\mu_{[\mathrm{mas} / \mathrm{yr}]}^{\mu_{\mathrm{f}_{2}}}$ | $\begin{gathered} \mathrm{F} \\ {[\mathrm{~mm}]} \end{gathered}$ | year |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0-1 | 18.024270 | 22.744107 | 0.00 | 0.00 | 18.002064 | 22.755148 | -3.57 | -8.12 | 15765 | 2011 |
| 0-2 | 18.024270 | 22.744107 | 0.00 | 0.00 | 18.042636 | 22.743713 | -5.48 | 2.30 | 15824 | 2011 |
| 0-3 | 18.024270 | 22.744107 | 0.00 | 0.00 | 18.013677 | 22.724062 | -4.44 | -26.81 | 15755 | 2011 |
| 0-4 | 18.024270 | 22.744107 | 0.00 | 0.00 | 17.973797 | 22.720838 | 9.26 | -4.07 | 15781 | 2011 |
| 0-1 | 15.690677 | 58.403094 | 0.00 | 0.00 | 15.671078 | 58.397176 | -33.78 | 0.87 | 15761 | 2011 |
| 0-2 | 15.690677 | 58.403094 | 0.00 | 0.00 | 15.696223 | 58.397288 | -6.16 | -13.82 | 15769 | 2011 |
| 0-3 | 15.690677 | 58.403094 | 0.00 | 0.00 | 15.683303 | 58.411670 | -4.40 | -1.35 | 15775 | 2011 |
| 0-4 | 15.690677 | 58.403094 | 0.00 | 0.00 | 15.685314 | 58.385840 | 1.86 | -2.47 | 15773 | 2011 |
| 0-5 | 15.690677 | 58.403094 | 0.00 | 0.00 | 15.690276 | 58.373386 | 0.16 | -1.28 | 15770 | 2011 |
| 0-6 | 15.690677 | 58.403094 | 0.00 | 0.00 | 15.706665 | 58.378832 | 30.57 | 13.97 | 15783 | 2011 |
| 0-1 | 343.280705 | 19.709619 | 0.00 | 0.00 | 343.270844 | 19.688776 | 7.53 | 2.00 | 15812 | 2011 |
| 0-2 | 343.280705 | 19.709619 | 0.00 | 0.00 | 343.254917 | 19.704537 | 26.80 | -5.09 | 15775 | 2011 |
| 0-3 | 343.280705 | 19.709619 | 0.00 | 0.00 | 343.277107 | 19.723909 | 45.25 | -3.12 | 15722 | 2011 |
| 0-4 | 343.280705 | 19.709619 | 0.00 | 0.00 | 343.297852 | 19.733495 | 0.06 | -14.81 | 15758 | 2011 |
| 0-5 | 343.280705 | 19.709619 | 0.00 | 0.00 | 343.308839 | 19.738109 | 6.73 | -0.82 | 15764 | 2011 |
| 0-6 | 343.280705 | 19.709619 | 0.00 | 0.00 | 343.316243 | 19.739516 | -4.73 | -3.72 | 15754 | 2011 |
| 0-10 | 343.280705 | 19.709619 | 0.00 | 0.00 | 343.235601 | 19.744564 | -6.24 | -12.42 | 15780 | 2011 |
| 0-1 | 344.322096 | 7.720084 | 0.00 | 0.00 | 344.314393 | 7.725902 | 16.93 | -12.71 | 15860 | 2011 |
| 0-2 | 344.322096 | 7.720084 | 0.00 | 0.00 | 344.299252 | 7.733080 | 0.37 | -0.88 | 15767 | 2011 |
| 0-3 | 344.322096 | 7.720084 | 0.00 | 0.00 | 344.291939 | 7.726671 | -3.45 | 0.04 | 15779 | 2011 |
| 0-4 | 344.322096 | 7.720084 | 0.00 | 0.00 | 344.340401 | 7.737714 | 7.81 | 4.88 | 15734 | 2011 |
| 0. 5 | 344.322096 | 7.720084 | 0.00 | 0.00 | 344.348585 | 7.724290 | 27.90 | -7.18 | 15753 | 2011 |
| 0-6 | 344.322096 | 7.720084 | 0.00 | 0.00 | 344.272324 | 7.730363 | -19.47 | -13.71 | 15779 | 2011 |
| 0. 8 | 344.322096 | 7.720084 | 0.00 | 0.00 | 344.319724 | 7.688006 | 9.70 | -8.88 | 15761 | 2011 |
| 0-9 | 344.322096 | 7.720084 | 0.00 | 0.00 | 344.322800 | 7.687318 | 22.00 | -23.82 | 15762 | 2011 |
| 1-2 | 1.392738 | 45.791748 | 6.47 | -5.84 | 1.420091 | 45.827052 | 13.85 | -7.68 | 15781 | 2005 |
| 1-2 | 1.392738 | 45.791748 | 6.47 | -5.84 | 1.420091 | 45.827052 | 13.85 | -7.68 | 15781 | 2006 |
| 1-2 | 1.392738 | 45.791748 | 6.47 | -5.84 | 1.420091 | 45.827052 | 13.85 | -7.68 | 15773 | 2010 |
| 1-2 | 1.392738 | 45.791748 | 6.47 | -5.84 | 1.420091 | 45.827052 | 13.85 | -7.68 | 15773 | 2011 |
| 1-2 | 1.392738 | 45.791748 | 6.47 | -5.84 | 1.420091 | 45.827052 | 13.85 | -7.68 | 15767 | 2012 |
| 1-3 | 1.392738 | 45.791748 | 6.47 | -5.84 | 1.452613 | 45.789707 | 6.68 | -8.17 | 15775 | 2005 |
| 1-3 | 1.392738 | 45.791748 | 6.47 | -5.84 | 1.452613 | 45.789707 | 6.68 | -8.17 | 15780 | 2006 |
| 1-3 | 1.392738 | 45.791748 | 6.47 | -5.84 | 1.452613 | 45.789707 | 6.68 | -8.17 | 15779 | 2010 |
| 1-3 | 1.392738 | 45.791748 | 6.47 | -5.84 | 1.452613 | 45.789707 | 6.68 | -8.17 | 15778 | 2011 |
| 1-3 | 1.392738 | 45.791748 | 6.47 | -5.84 | 1.452613 | 45.789707 | 6.68 | -8.17 | 15780 | 2012 |
| 2-3 | 1.420091 | 45.827052 | 13.85 | -7.68 | 1.452613 | 45.789707 | 6.68 | -8.17 | 15773 | 2005 |
| 2-3 | 1.420091 | 45.827052 | 13.85 | -7.68 | 1.452613 | 45.789707 | 6.68 | -8.17 | 15781 | 2006 |
| 2-3 | 1.420091 | 45.827052 | 13.85 | -7.68 | 1.452613 | 45.789707 | 6.68 | -8.17 | 15773 | 2010 |
| 2-3 | 1.420091 | 45.827052 | 13.85 | -7.68 | 1.452613 | 45.789707 | 6.68 | -8.17 | 15772 | 2011 |
| 2-3 | 1.420091 | 45.827052 | 13.85 | -7.68 | 1.452613 | 45.789707 | 6.68 | -8.17 | 15767 | 2012 |
| $15774 \pm 21$ |  |  |  |  |  |  |  |  |  |  |

